Wide distribution of regular pattern wavenumbers in model and real ecosystems

Robbin Bastiaansen

2018-02-14: NAEM 2018

Universiteit Leiden
The Netherlands

Other people involved:		
Mathematicians	*Ecologists (theorists)*	*Ecologists (data scientists)*
❖ Olfa Jaïbi	❖ Koen Siteur	❖ Vincent Deblauwe
❖ Eric Siero	❖ Maarten Eppinga	❖ Stephane Mermoz
❖ Arjen Doelman	❖ Max Rietkerk	❖ Alexandre Bouvet

Patterns are omnipresent in dryland ecosystems

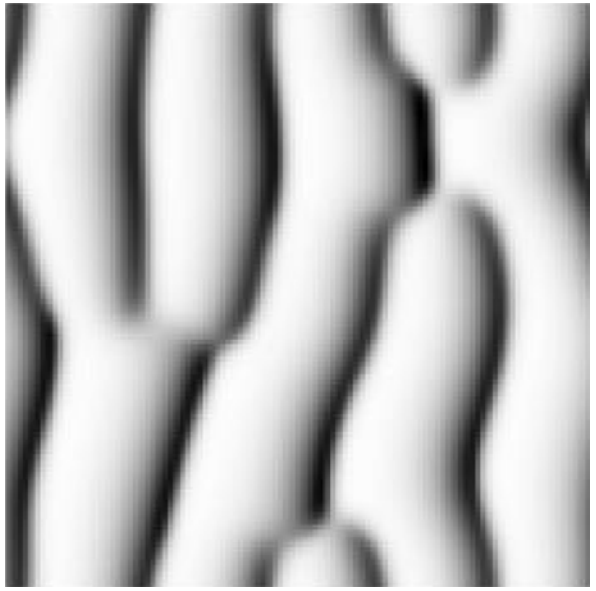
Somaliland, 1948
Source: W. A. Macfadyen, *1950*

Somaliland, 2017
Source: Google Earth, 2017

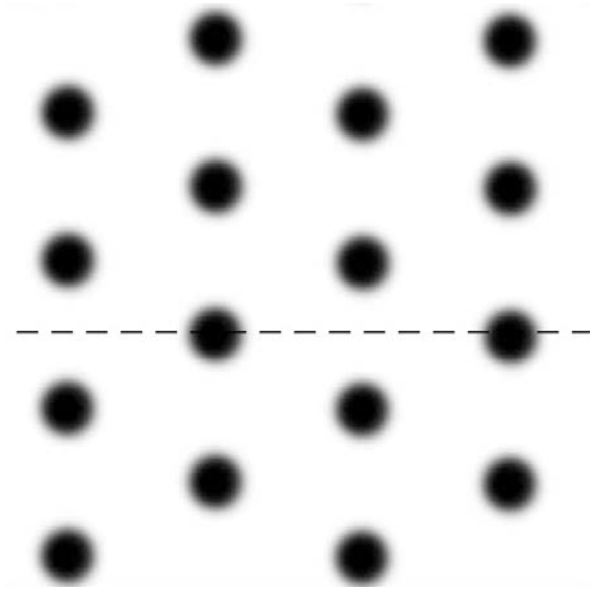
Reaction-diffusion equations model ecosystems

Archetype model: extended-Klausmeier model

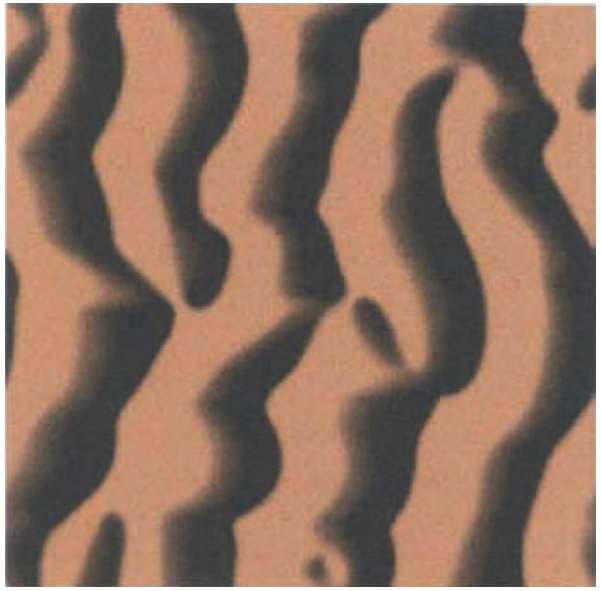
$$\begin{cases} \dfrac{\partial w}{\partial t} &= e\dfrac{\partial^2 w}{\partial x^2} + \dfrac{\partial (vw)}{\partial x} + a - w - wn^2 \\ \dfrac{\partial n}{\partial t} &= \dfrac{\partial^2 n}{\partial x^2} - mn + wn^2 \end{cases}$$



Source: Klausmeier, 1999

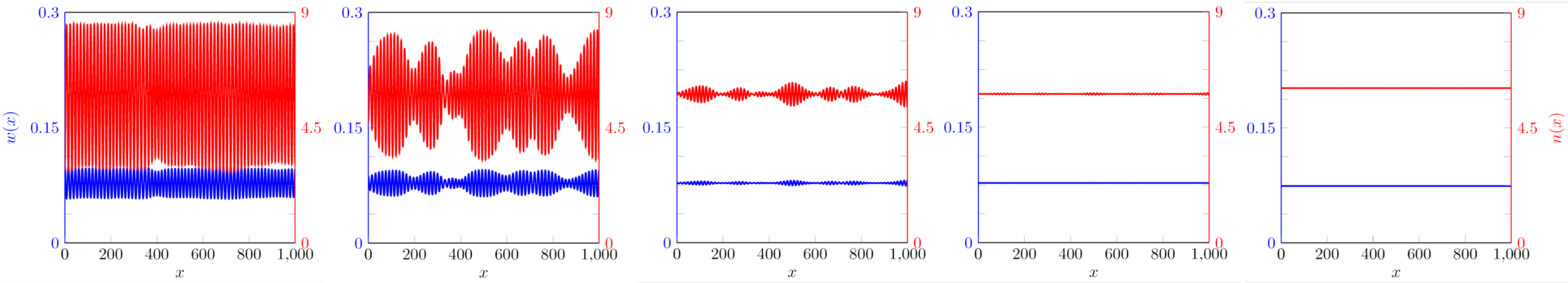


Source: Gilad et al, 2004



Source: Rietkerk et al, 2002

The origin of patterns in reaction-diffusion models



Low rainfall

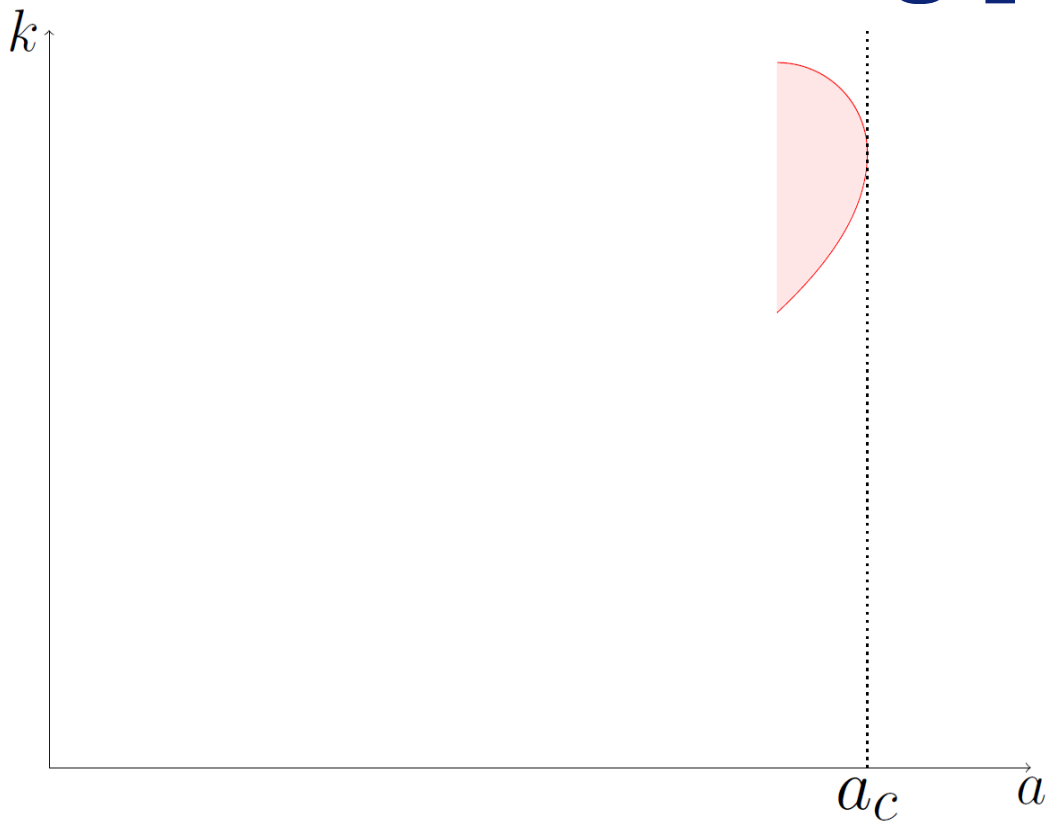
Critical rainfall
Onset of patterns

High rainfall

Turing Patterns [Turing, 1952]

Found in most reaction-diffusion equations

Wavenumbers of Turing patterns



Eckhaus/Benjamin-Feir-Newell instability criterion

[Eckhaus, 1965; Benjamin & Feir, 1967; Newell, 1974]

Determination of the stable Turing patterns

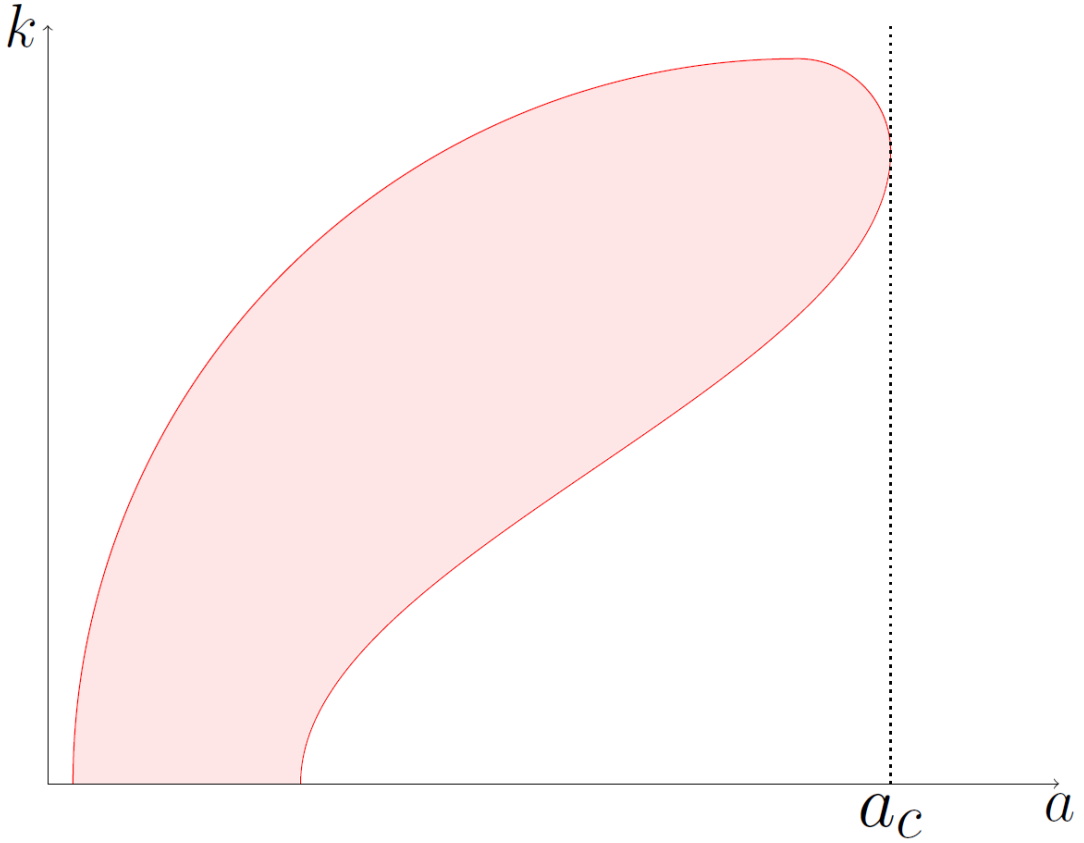
Rayleigh Bénard thermal convection

Busse balloon [Busse, 1978]

A *Busse balloon* is a model-dependent shape in (*parameter*, *wavenumber*)-space that indicates all combinations of parameter and wavenumber that represent stable solutions of the model.

Video source: wikiRigaou (wikimedia commons)

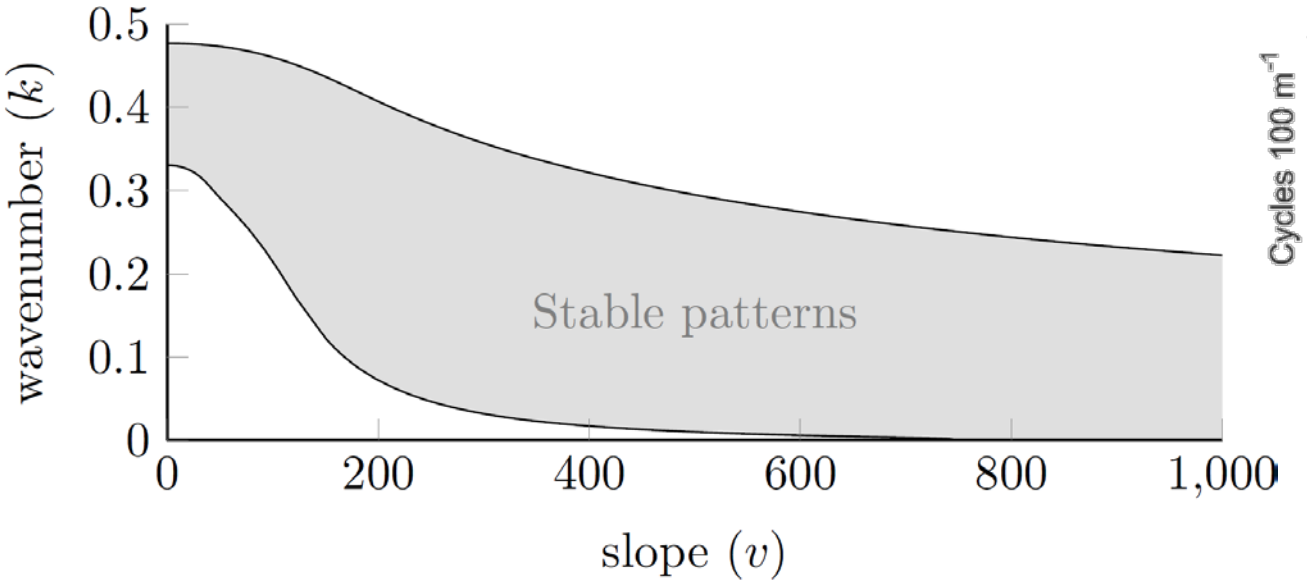
Busse balloon in the extended-Klausmeier



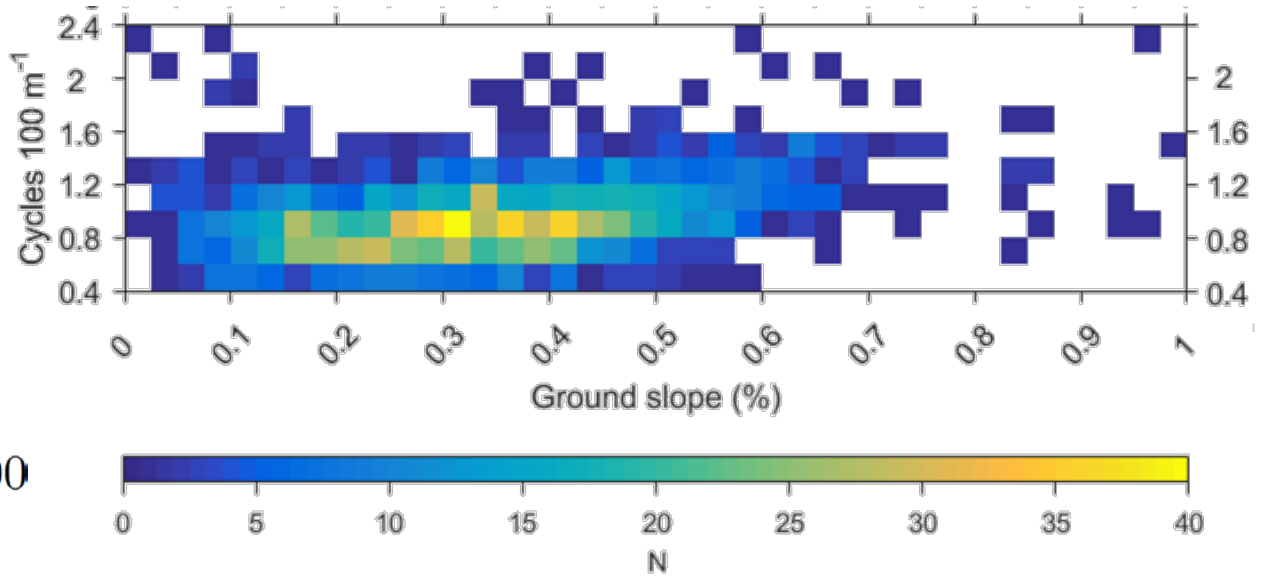
Continuation software

Advanced numerics is required to compute the Busse balloon

Busse balloon in dryland ecosystems



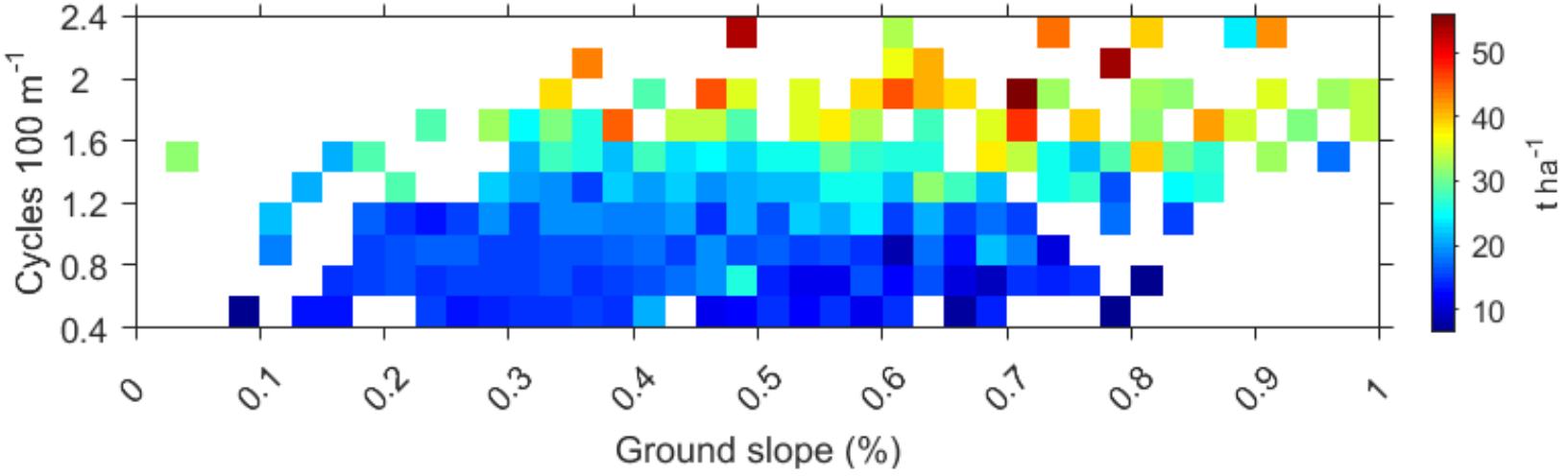
extended-Klausmeier model



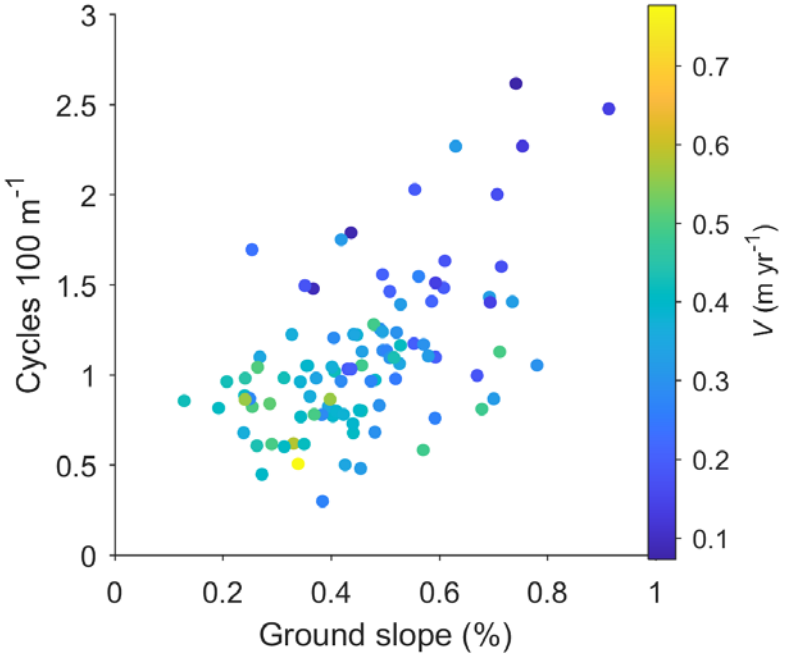
Somaliland data

Wide wavenumber spread in both!

Wavenumber influences state variables



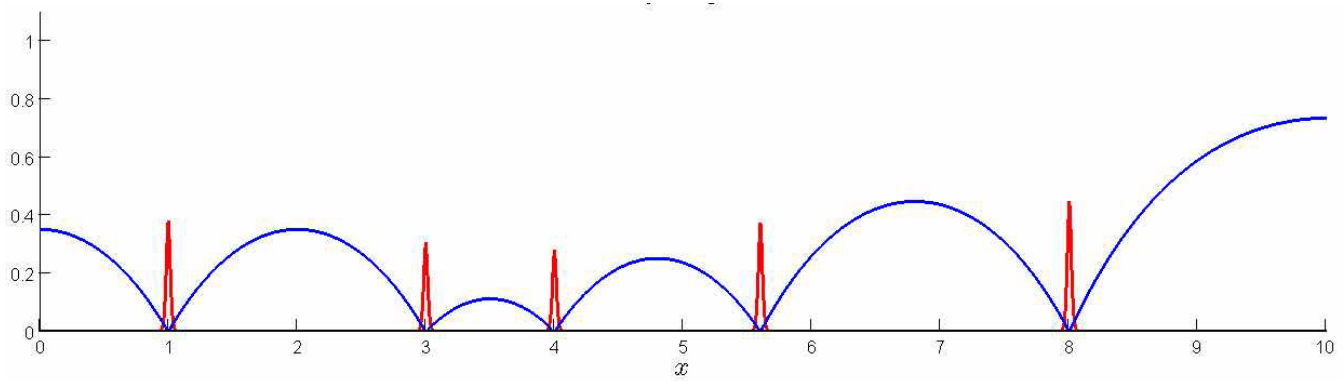
Biomass data

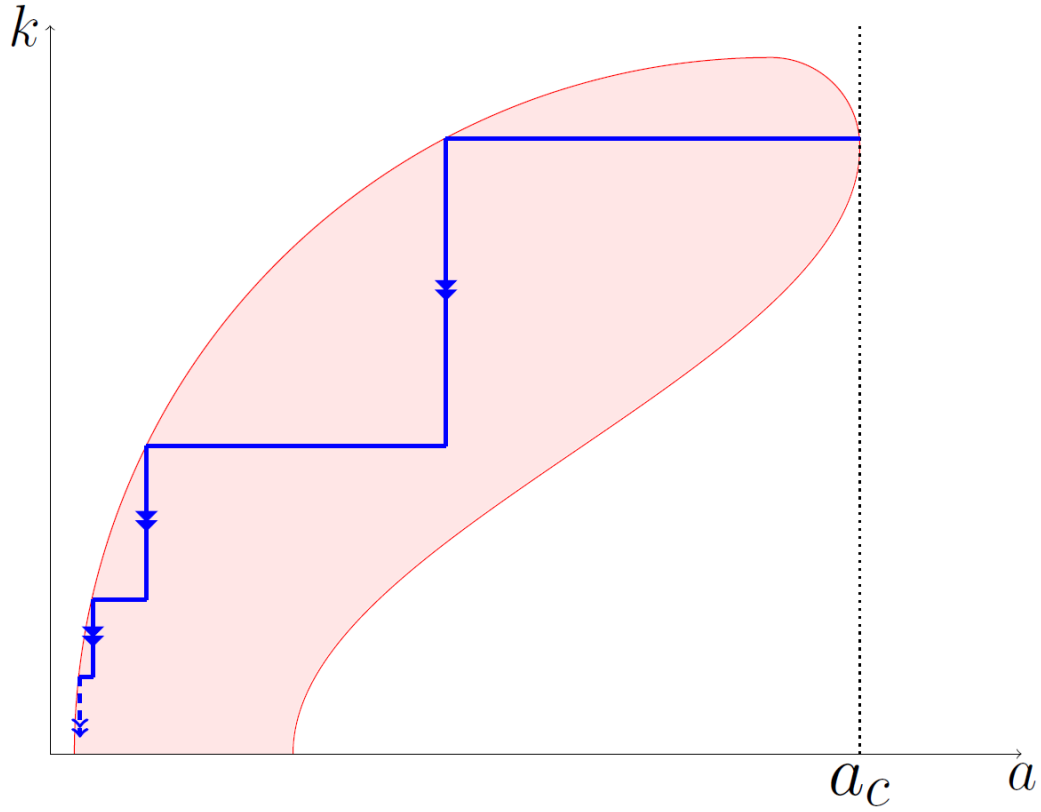


Migration speed data

Biomass and migration speed change with wavenumber!

Enhanced resilience through self-organisation?



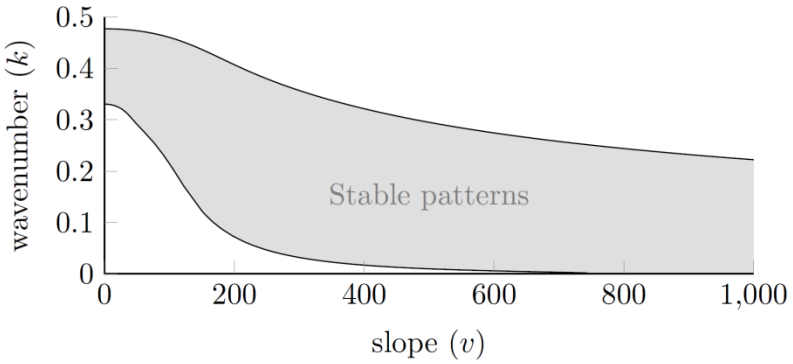


Pulse rearangement

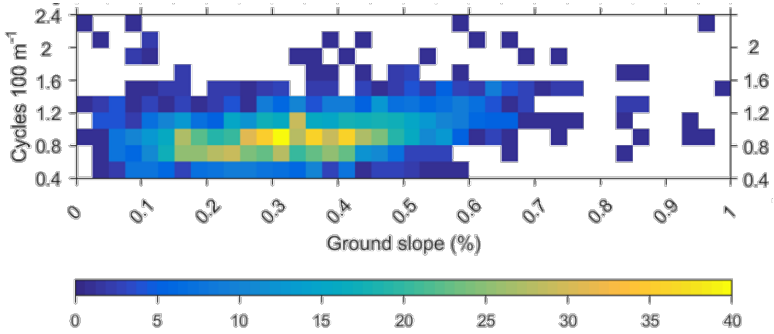
Wavelenght adaption

Bastiaansen & Doelman, *submitted*

Siteur et al, 2014



Conclusions



Wide wavenumber spread in model and real dryland ecosystems

implies

Biomass and migration speed change with wavenumber

and suggests

Enhanced resilience through self-organisation via ...

Pulse rearangement & Wavelenght adaption