

# Multistability of model and real dryland ecosystems through spatial self-organization

Robbin Bastiaansen

2019-06-06



Universiteit  
Leiden  
The Netherlands

## Other people involved:

### *Mathematicians*

- ❖ Olfa Jaïbi
- ❖ Eric Siero
- ❖ Arjen Doelman

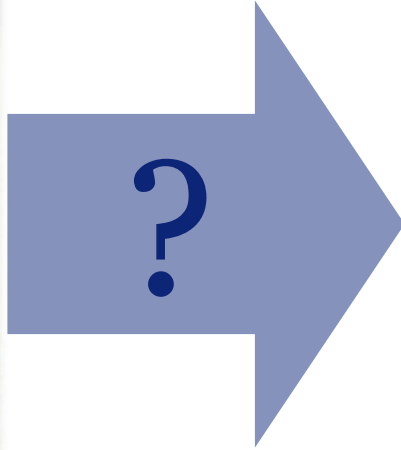
### *Ecologists (theorists)*

- ❖ Koen Siteur
- ❖ Maarten Eppinga
- ❖ Max Rietkerk

### *Ecologists (data scientists)*

- ❖ Vincent Deblauwe
- ❖ Stephane Mermoz
- ❖ Alexandre Bouvet

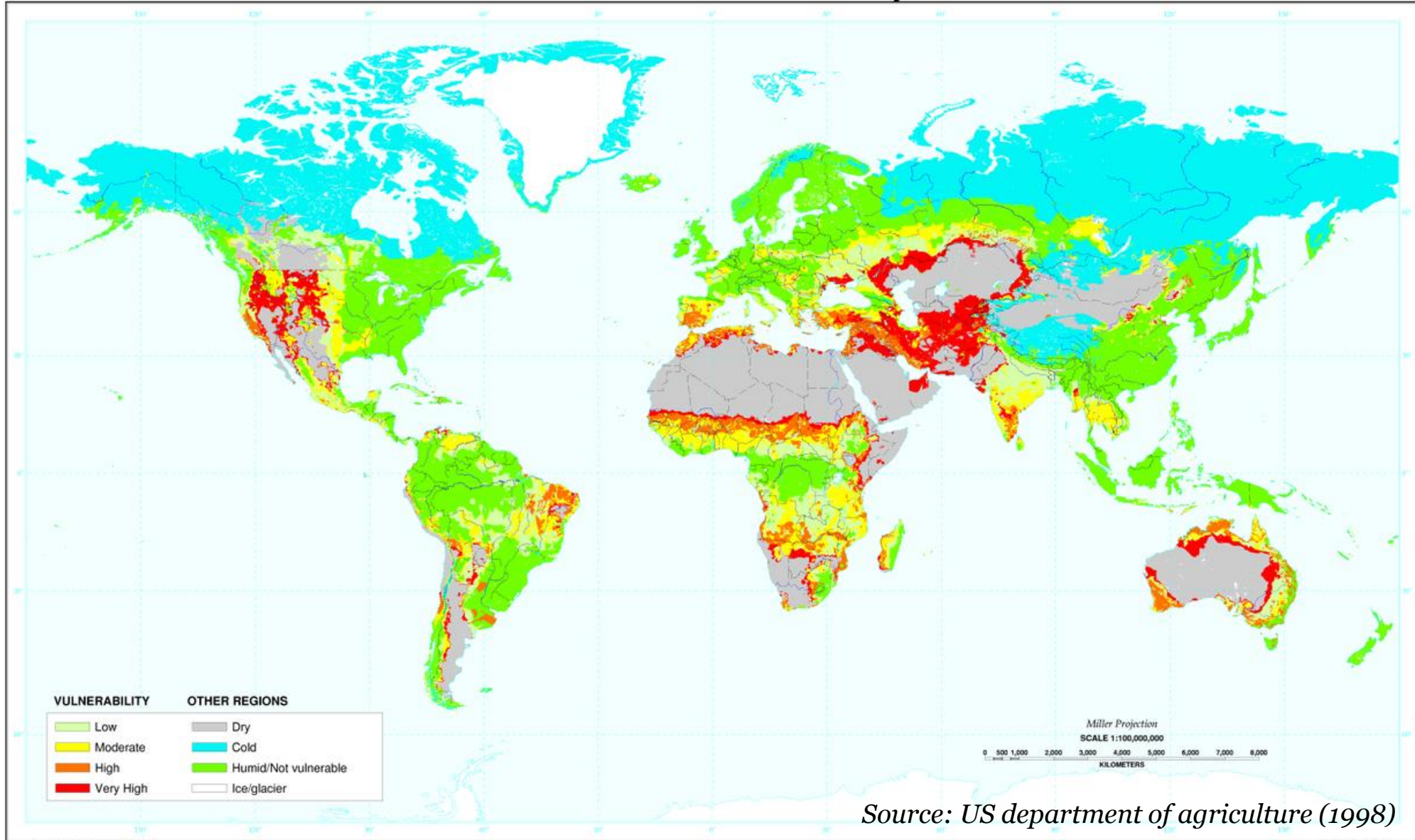
# The desertification process



# Desertification vulnerability

U.S. Department of Agriculture  
Natural Resources Conservation Service  
Soil Survey Division  
World Soil Resources

## Desertification Vulnerability

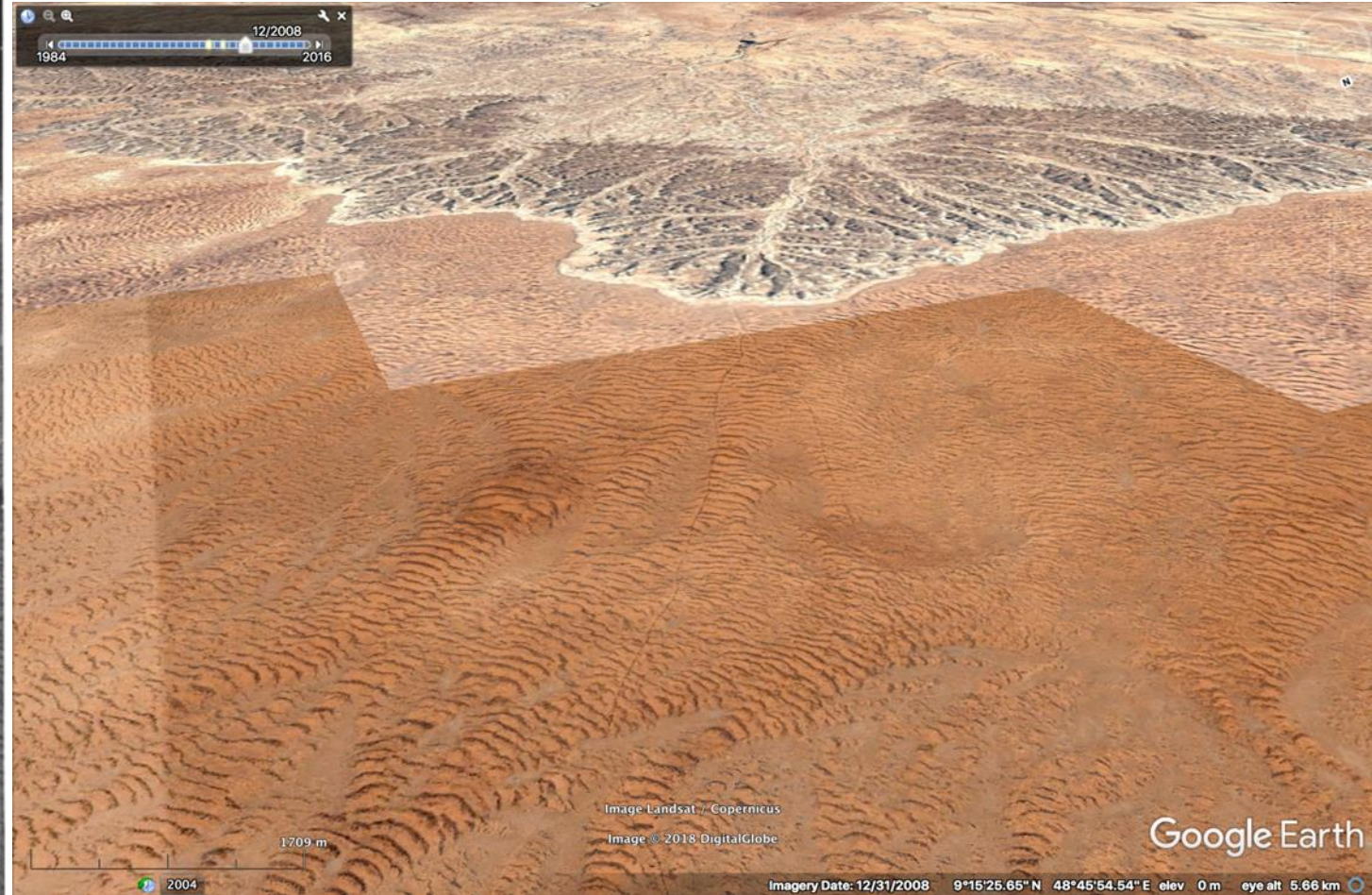


Source: US department of agriculture (1998)

# Patterns are omnipresent in dryland ecosystems



Somaliland, 1948  
Source: W. A. Macfadyen, 1950

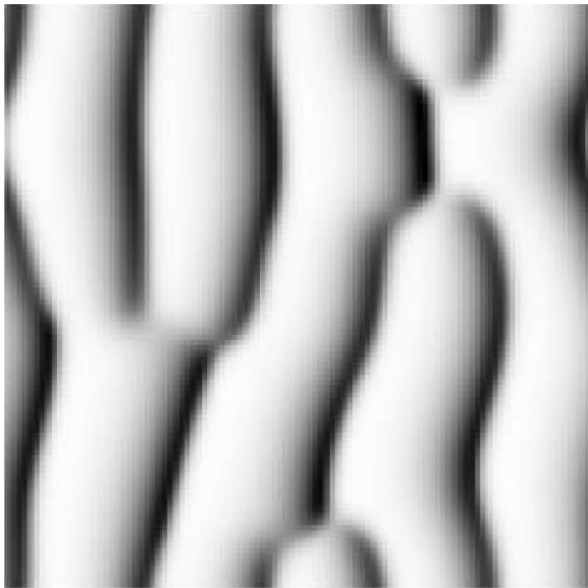


Somaliland, 2008  
Source: Google Earth, 2018

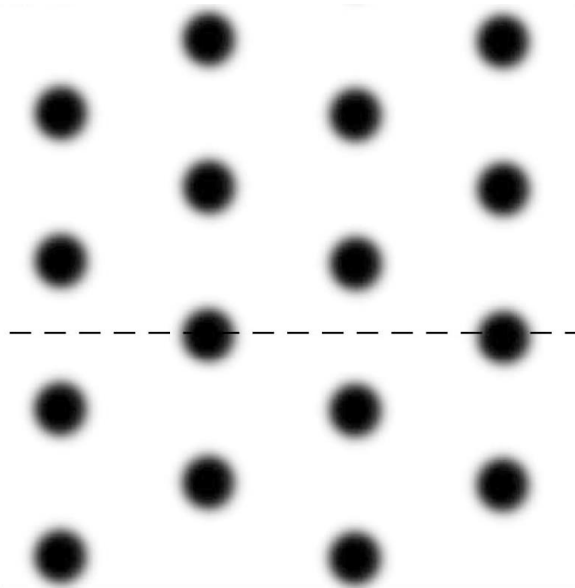
# Reaction-diffusion equations model ecosystems

Archetype model: extended-Klausmeier model

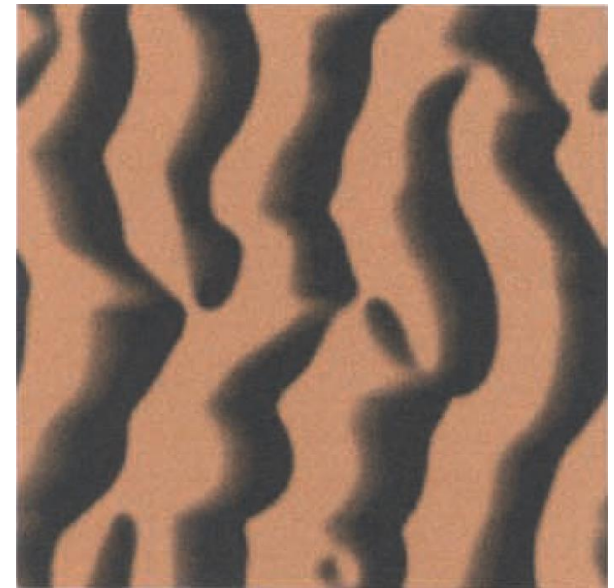
$$\begin{cases} \frac{\partial w}{\partial t} &= e \frac{\partial^2 w}{\partial x^2} + \frac{\partial(vw)}{\partial x} + a - w - wn^2 \\ \frac{\partial n}{\partial t} &= \frac{\partial^2 n}{\partial x^2} - mn + wn^2 \end{cases}$$



Source: Klausmeier, 1999

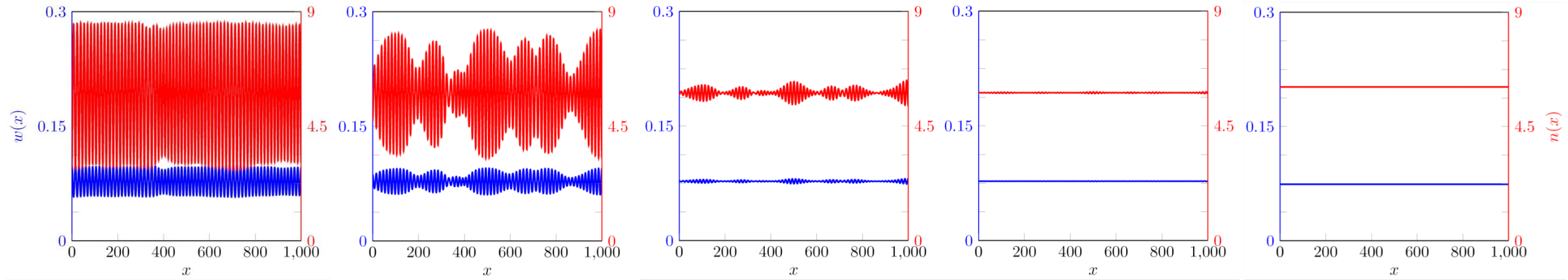


Source: Gilad et al, 2004



Source: Rietkerk et al, 2002

# The origin of patterns in reaction-diffusion models



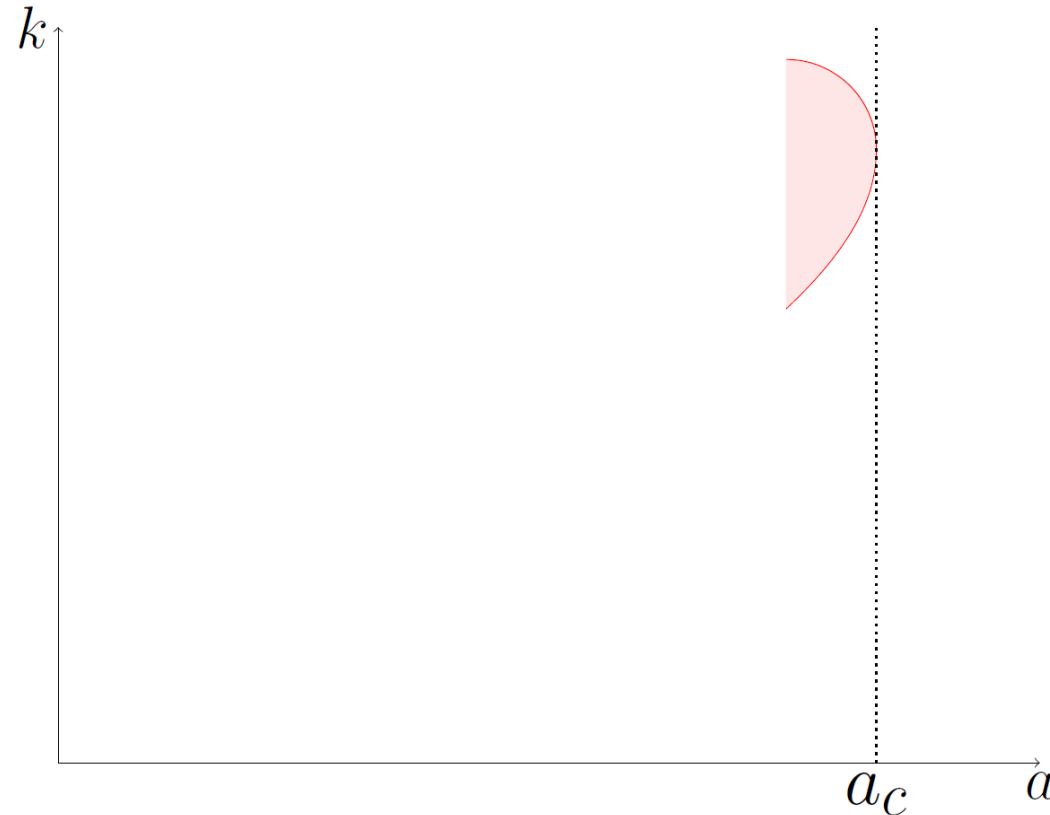
Low rainfall

Critical rainfall  
Onset of patterns

High rainfall

**Turing Patterns** [Turing, 1952]  
Found in most reaction-diffusion equations

# Wavenumbers of Turing patterns

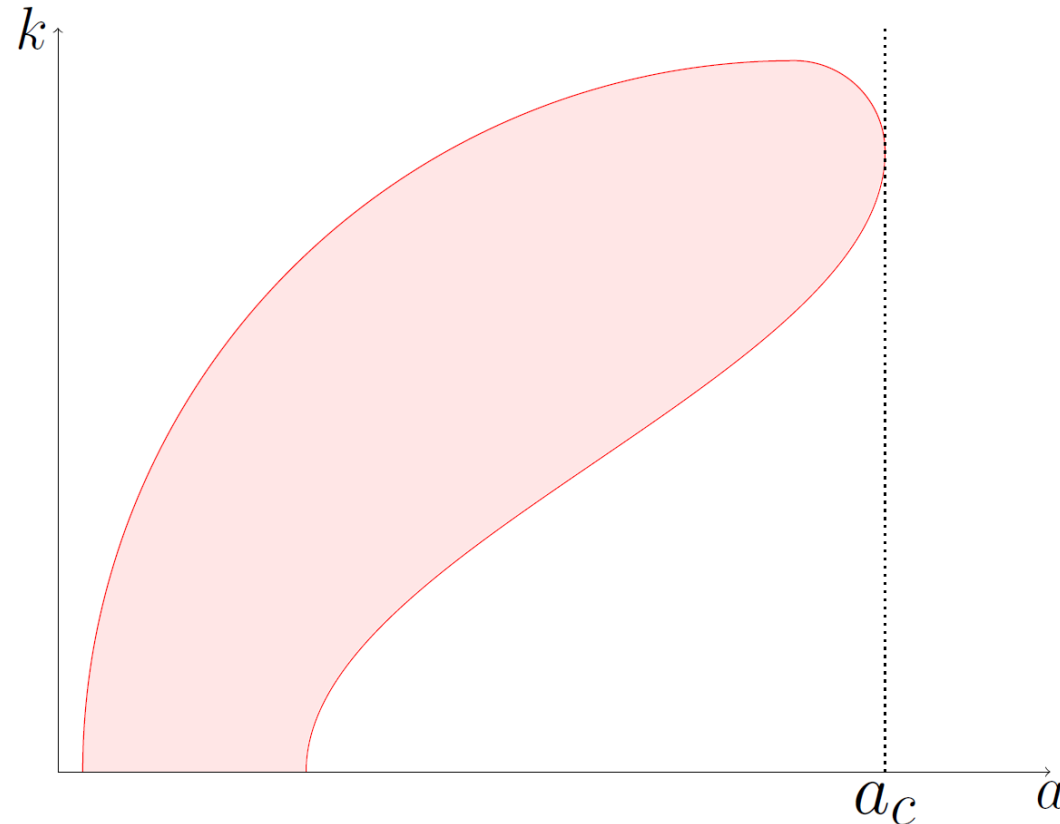


## Eckhaus/Benjamin-Feir-Newell instability criterion

[Eckhaus, 1965; Benjamin & Feir, 1967; Newell, 1974]

Determination of the stable Turing patterns

# Busse balloon

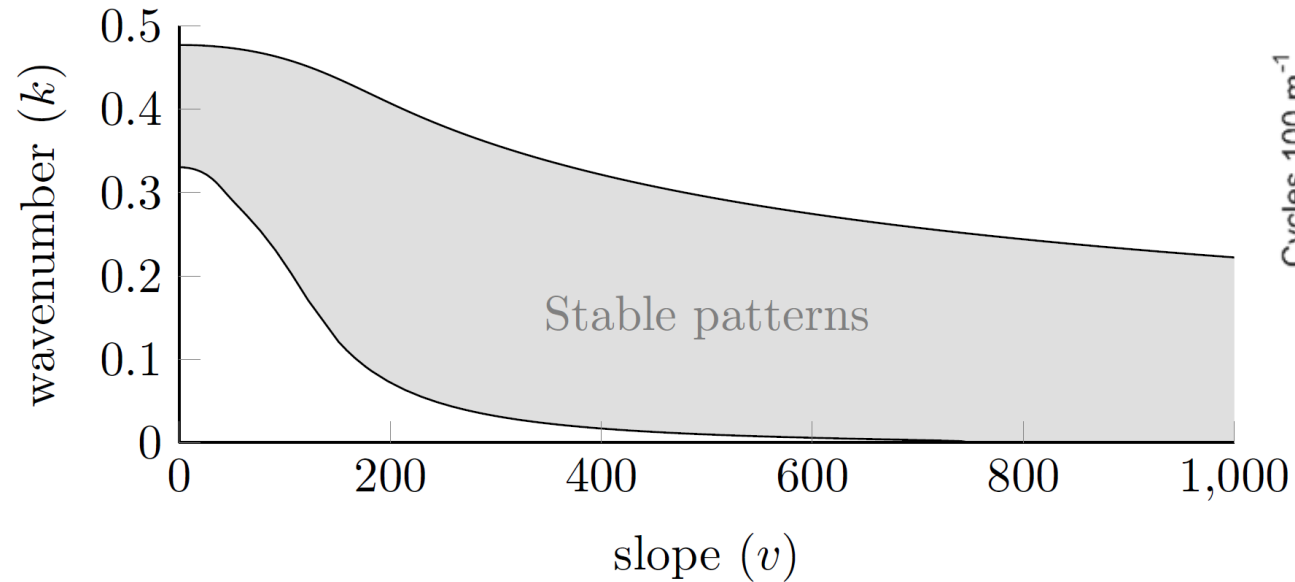


## Busse balloon [Busse, 1978]

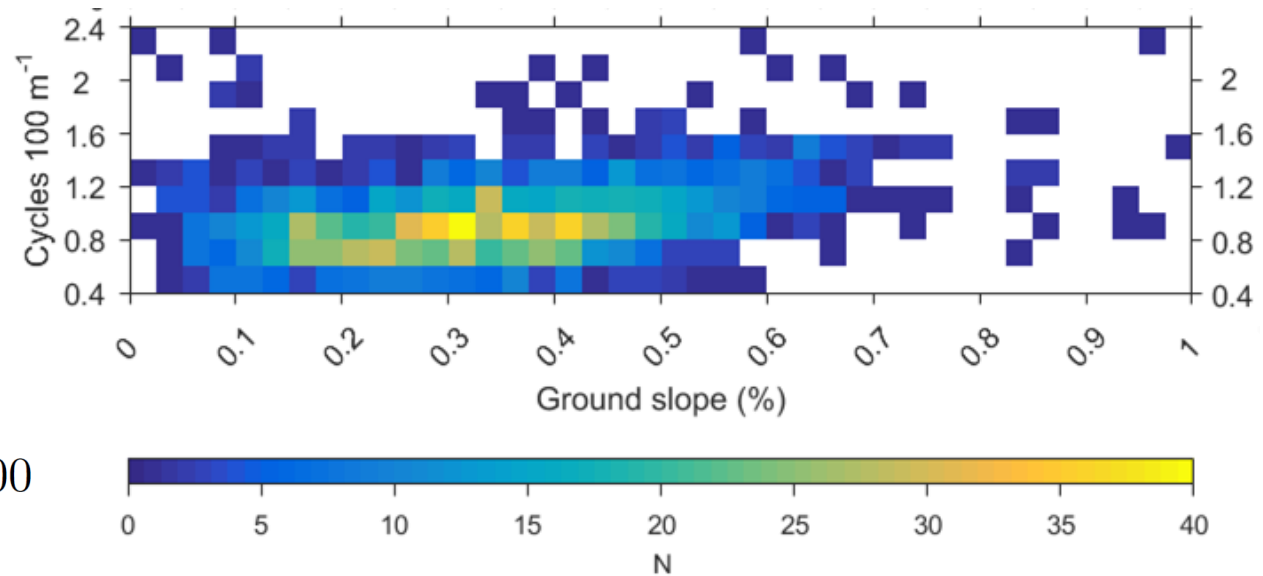
A *Busse balloon* is a model-dependent shape in  $(parameter, wavenumber)$ -space that indicates all combinations of parameter and wavenumber that represent stable solutions of the model



# Busse balloon in dryland ecosystems



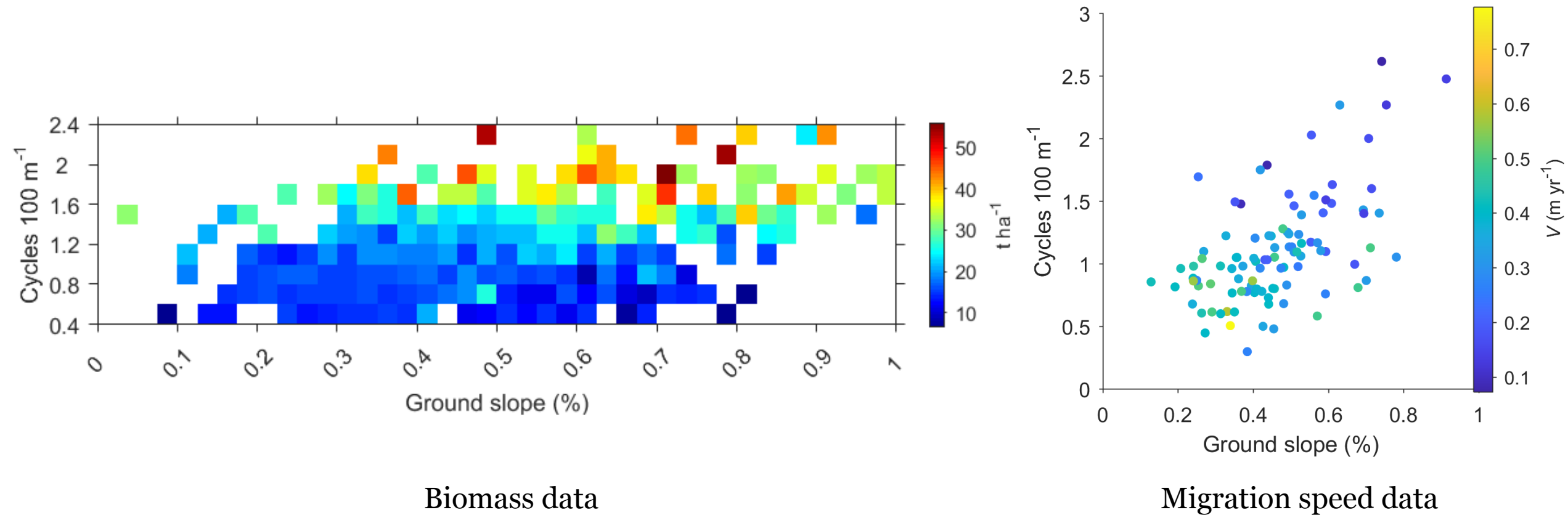
extended-Klausmeier model



Somaliland data

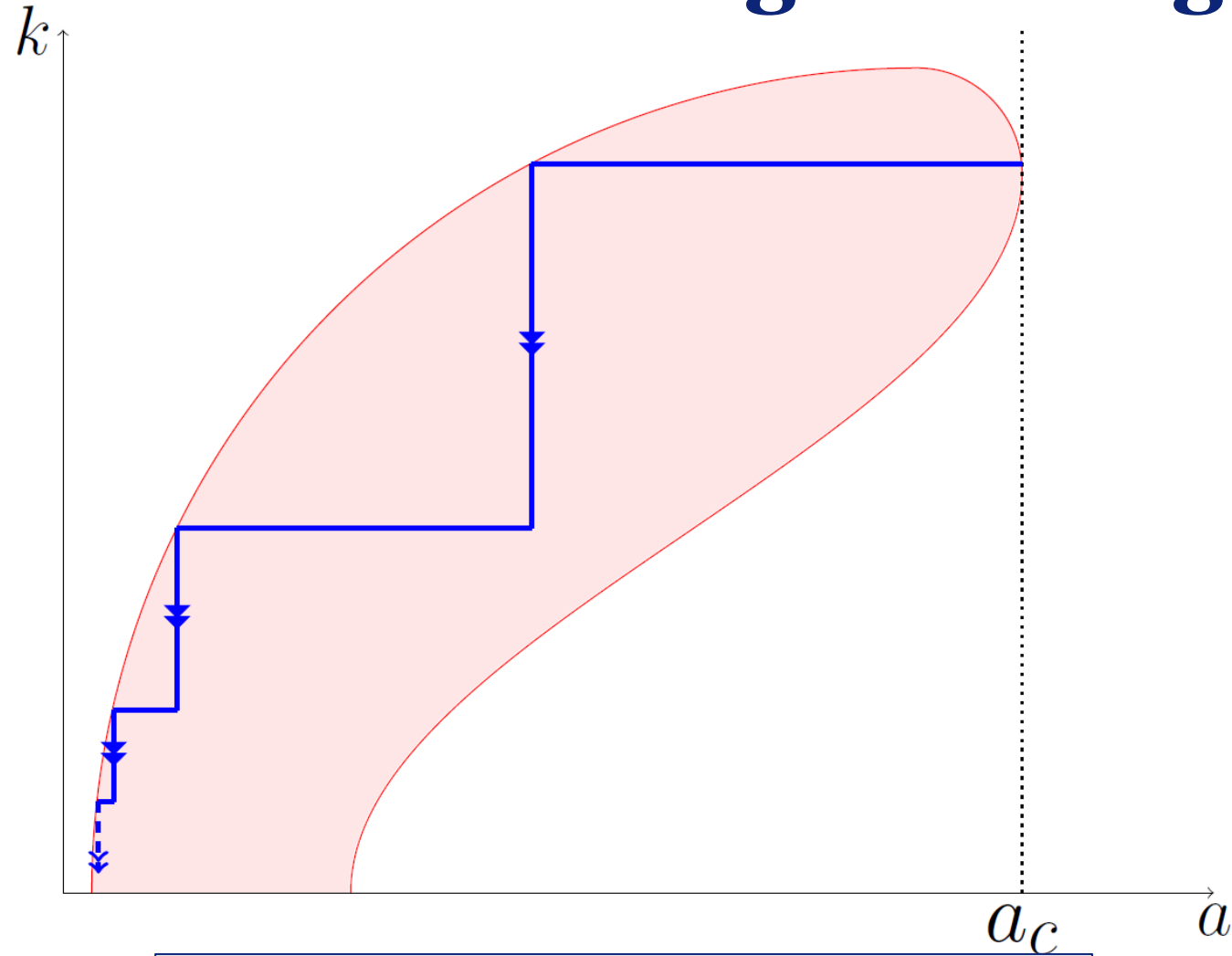
Wide wavenumber spread in both!

# Wavenumber influences state variables



Biomass and migration speed change with wavenumber!

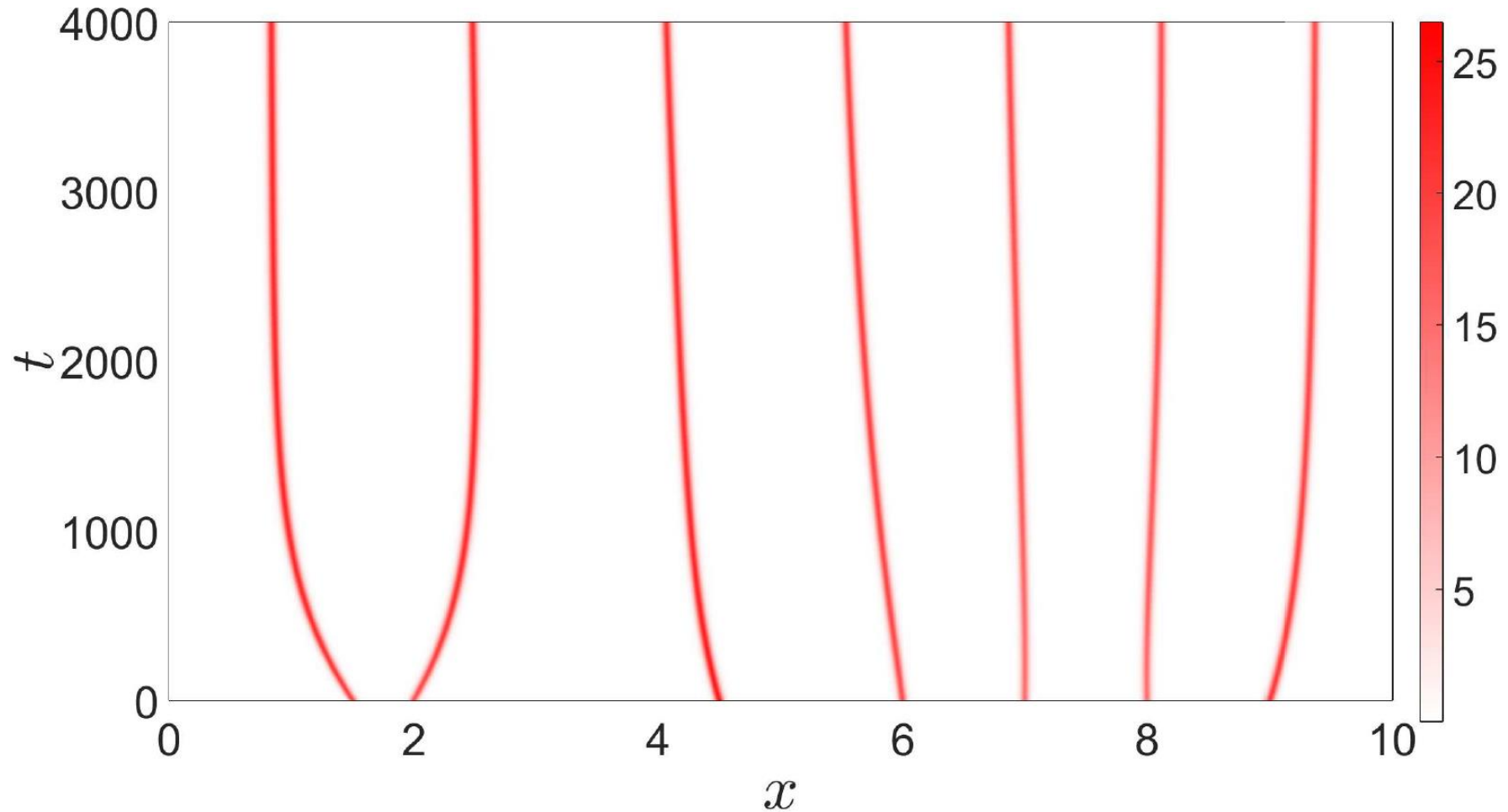
# Enhanced resilience through self-organisation?



Wavelength adaption

Siteur et al, 2014

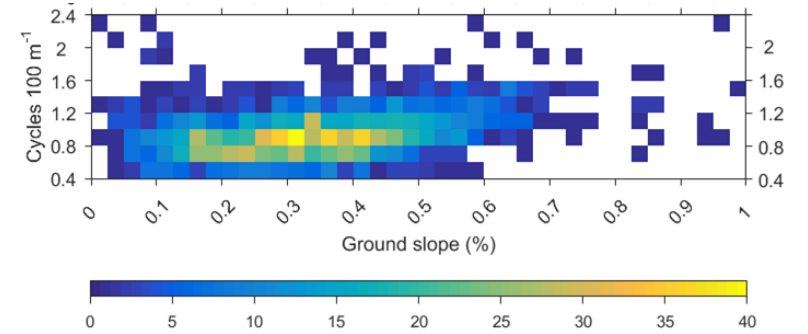
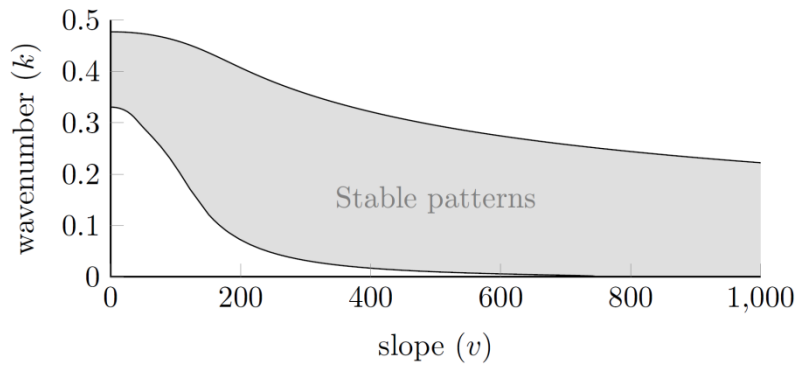
# Enhanced resilience through self-organisation?



Pulse rearrangement

Bastiaansen & Doelman, *submitted*

# Conclusions



**Wide wavenumber spread in model and real dryland ecosystems**

implies

Biomass and migration speed change with wavenumber

and suggests

Enhanced resilience through self-organisation via ...

Wavelength adaption

&

Pulse rearrangement

