

# Projections of the Transient State-Dependency of Climate Feedbacks

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# Summary

## Climate Feedbacks

Warming leads to change of internal process of climate system

- ☀ Planck radiation feedback
- ☁ Surface Albedo feedback
- 🌡 Lapse Rate feedback
- 💧 Water Vapour feedback
- ☁ Cloud Formation feedback

## Problem:

Classic methods relate everything linearly to global warming

- 😞 Misses state-dependency and changes in feedback strength

## Solution:

Decomposition of feedbacks as observables over time scales

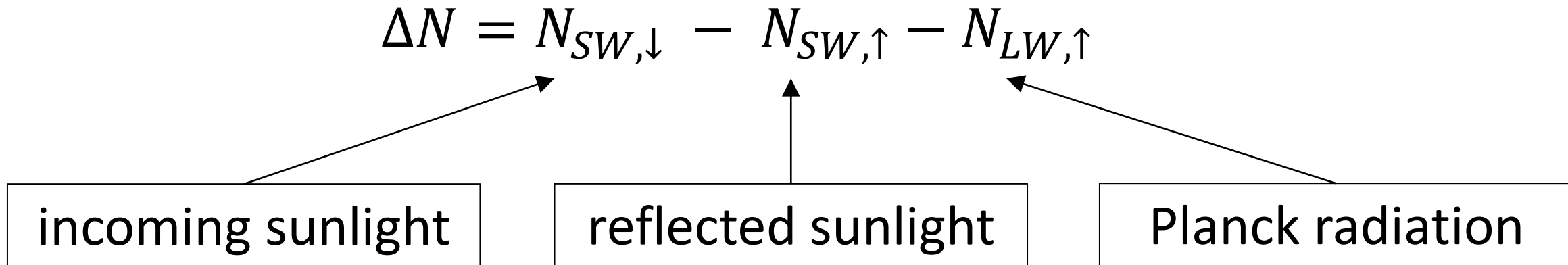
- 🕒 Captures temporal evolution & state-dependency of feedbacks



# **Climate Feedback Theory**

# Classic treatment of climate feedbacks (1)

Warming is due to net positive radiative imbalance



When  $\Delta N = 0$  no more warming:

→ equilibrium warming  $\Delta T_* = T_* - T_0$

# Classic treatment of climate feedbacks (2)

Express imbalance as function of system state

$$\Delta N(t) = \Delta \tilde{N}(y(t), \mu(t))$$

Near equilibrium  $y_*$  (with  $\mu = \mu_*$ ) a Taylor expansion gives

$$\Delta N(t) = \Delta \tilde{N}(y_*, \mu_*) + \left. \frac{\partial \Delta \tilde{N}}{\partial \mu} \right|_* \Delta \mu(t) + \left. \frac{\partial \Delta \tilde{N}}{\partial y} \right|_* \Delta y(t) + h.o.t.$$

Equals Zero

Radiative Forcing

Climate Response

*Assumed to be small*

$$\Delta N(t) = F(t) + \Delta R(t)$$

**Implicit assumption:** relevant climate dynamics are **approximately a linear system**

# Classic treatment of climate feedbacks (3)

Climate Response  $\Delta R$  is sum of *feedback contributions*:

$$\Delta R(t) = \sum_{j \in \mathcal{F}} \Delta R_j(t)$$

$\mathcal{F}$  is set of **Climate Feedbacks**:

- ☀ Planck radiation feedback
- ☁ Surface Albedo feedback
- 🌡 Lapse Rate feedback
- 💧 Water Vapour feedback
- ☁ Cloud Formation feedback

$$\Delta R_j(t) := \left. \frac{\partial \Delta N}{\partial y_j} \right|_* \Delta y_j(t)$$

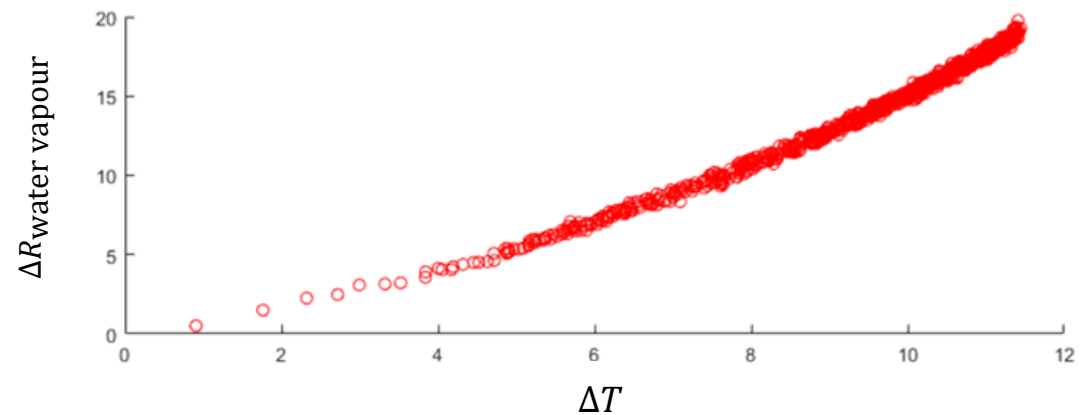
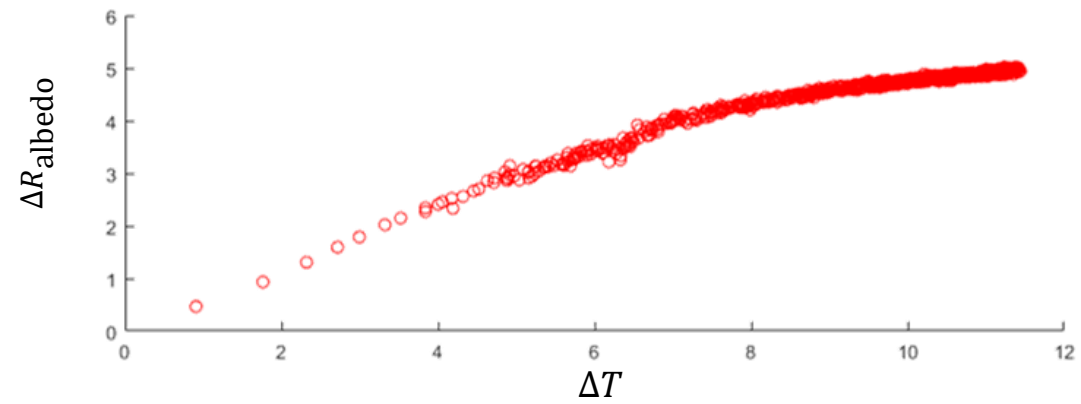
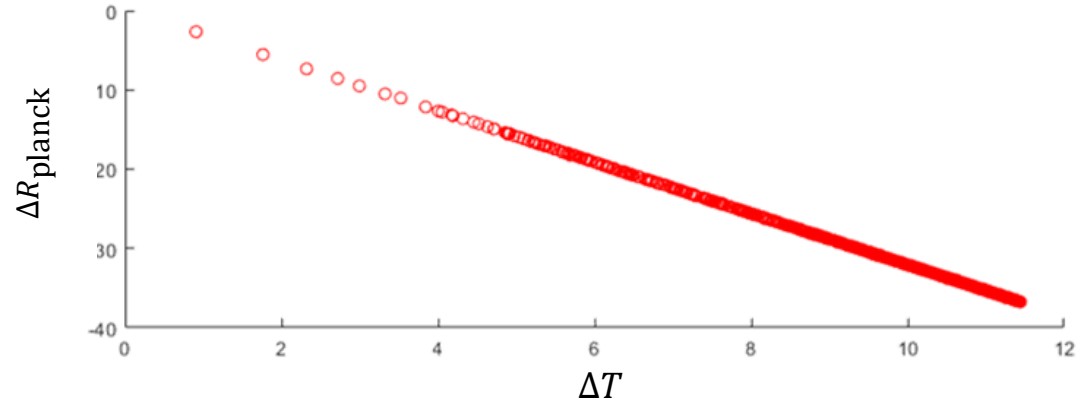
Classic: define feedback strength  $\lambda_j$  via

$$\Delta R_j(t) = \lambda_j \Delta T(t)$$

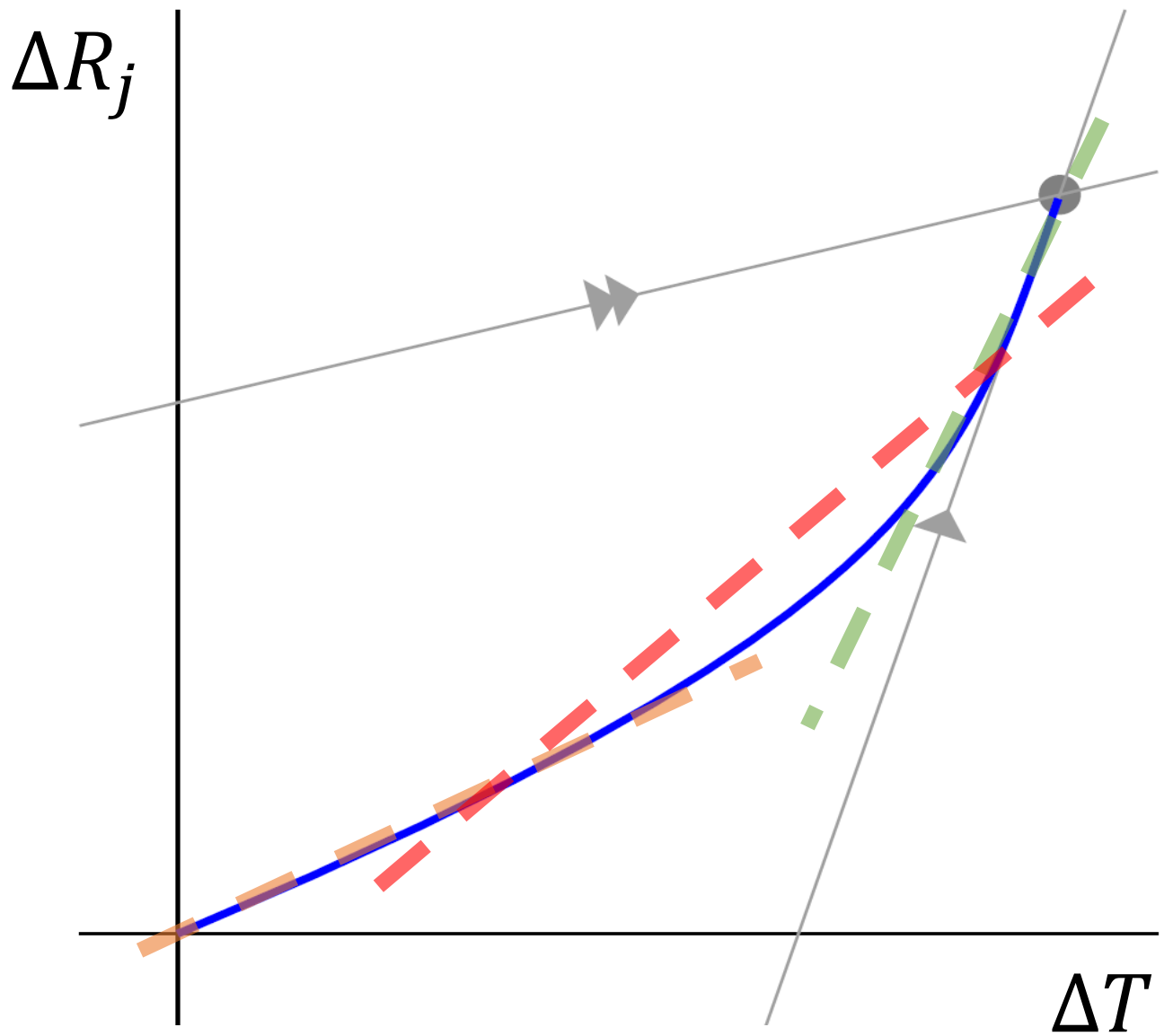
Pre-computed radiative kernel

**Implicit assumption:** relevant climate dynamics play on **approximately one mode**

# The problem with the classic treatment (1)



# The problem with the classic treatment (2)





# Evolution of Observables

Linear Response Theory (& Koopman Theory):

$$\frac{dO}{dt} = \mathcal{L}O + g(t)$$

$$\Delta O(t) = (G^{[O]} * g)(t) = \int_0^t G^{[O]}(s) g(t-s) ds$$

Approximation of Green Function:

$$G^{[O]}(t) = \sum_{m=1}^M \beta_m^{[O]} e^{-t/\tau_m}$$

So:

$$\Delta O(t) = \sum_{m=1}^M \beta_m^{[O]} \mathcal{M}_m^g(t)$$

$$\mathcal{M}_m^g(t) = \int_0^t e^{-s/\tau_m} g(t-s) ds$$

all  
observable  
dependency

all  
forcing (and time)  
dependency

# New feedback metrics

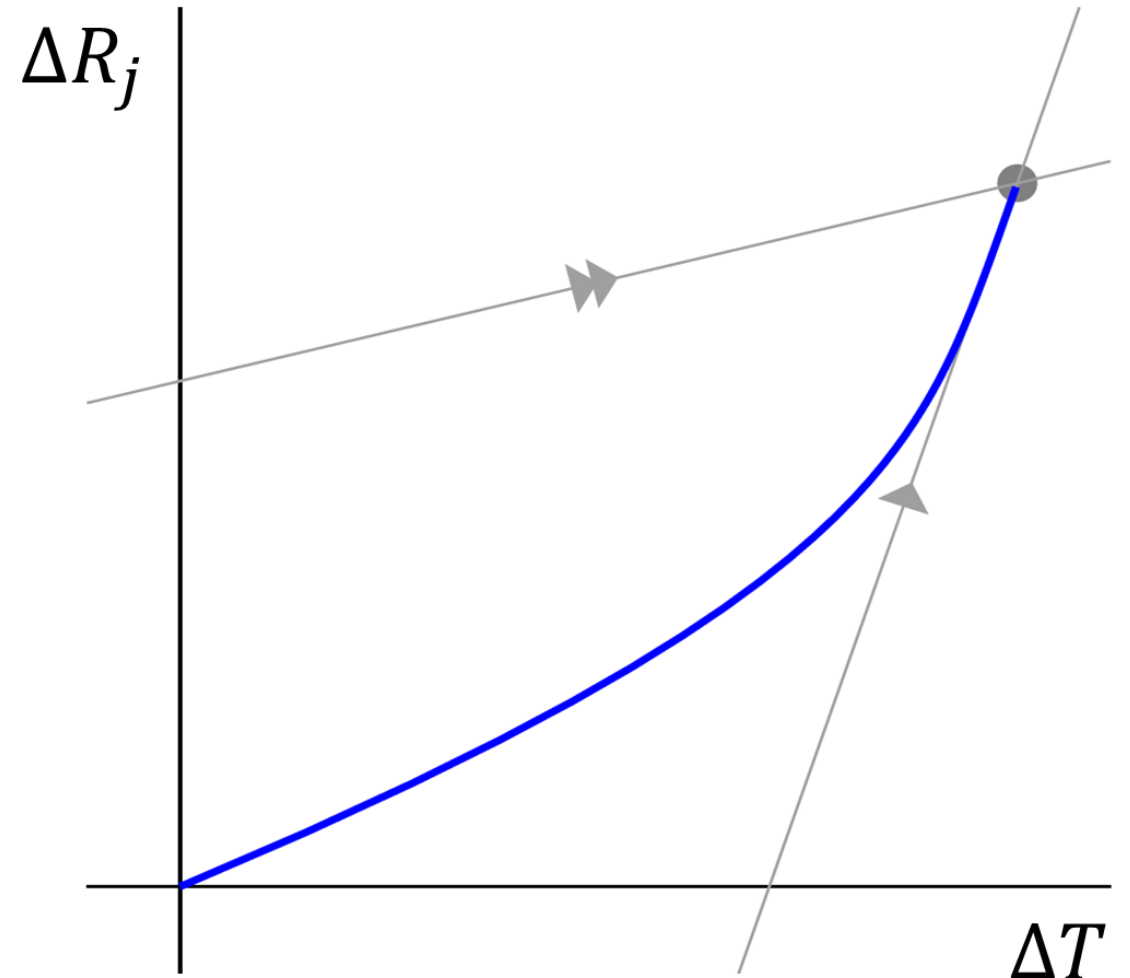
Feedback strength per mode:

$$\lambda_j^m := \frac{\beta_m^{[R_j]}}{\beta_m^{[T]}}$$

Instantaneous feedback strength:

$$\lambda_j^{inst}(t) := \frac{\frac{d}{dt}\Delta R_j(t)}{\frac{d}{dt}\Delta T(t)}$$

$$\Delta O(t) = \sum_{m=1}^M \beta_m^{[O]} \mathcal{M}_m^g(t)$$





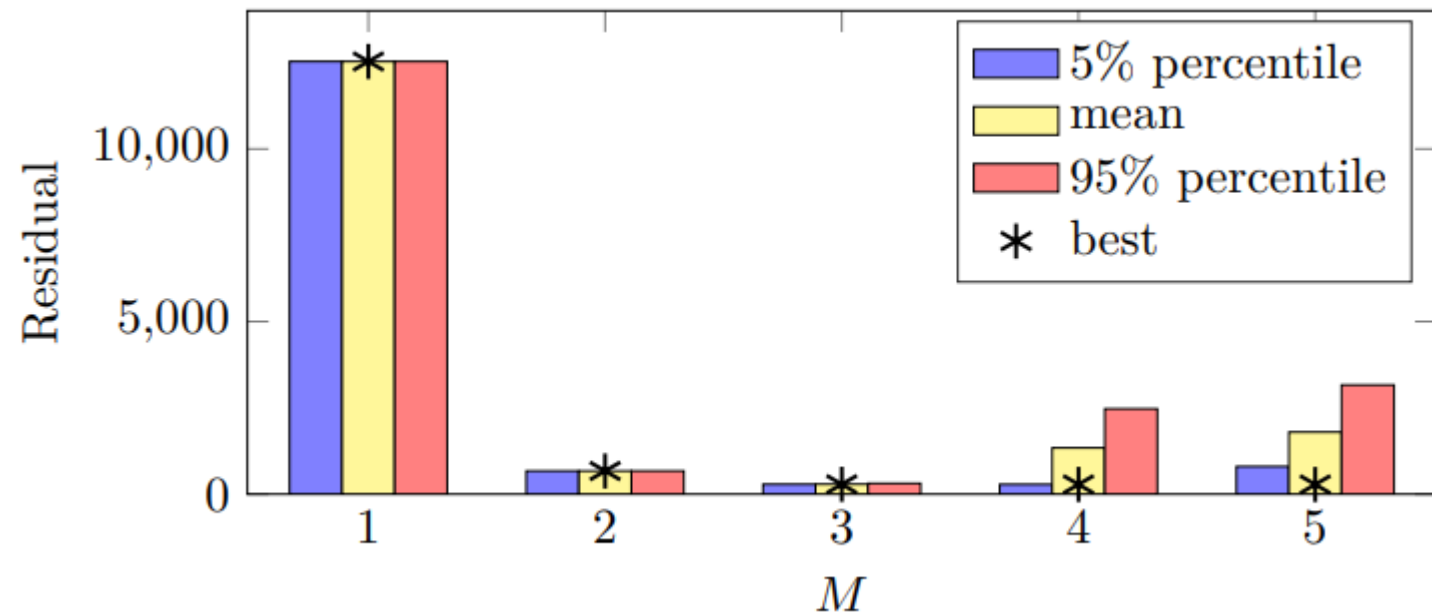
# **Application to CESM2 runs**

# Application to CESM2's abrupt4xCO2 run in CMIP6 (1)

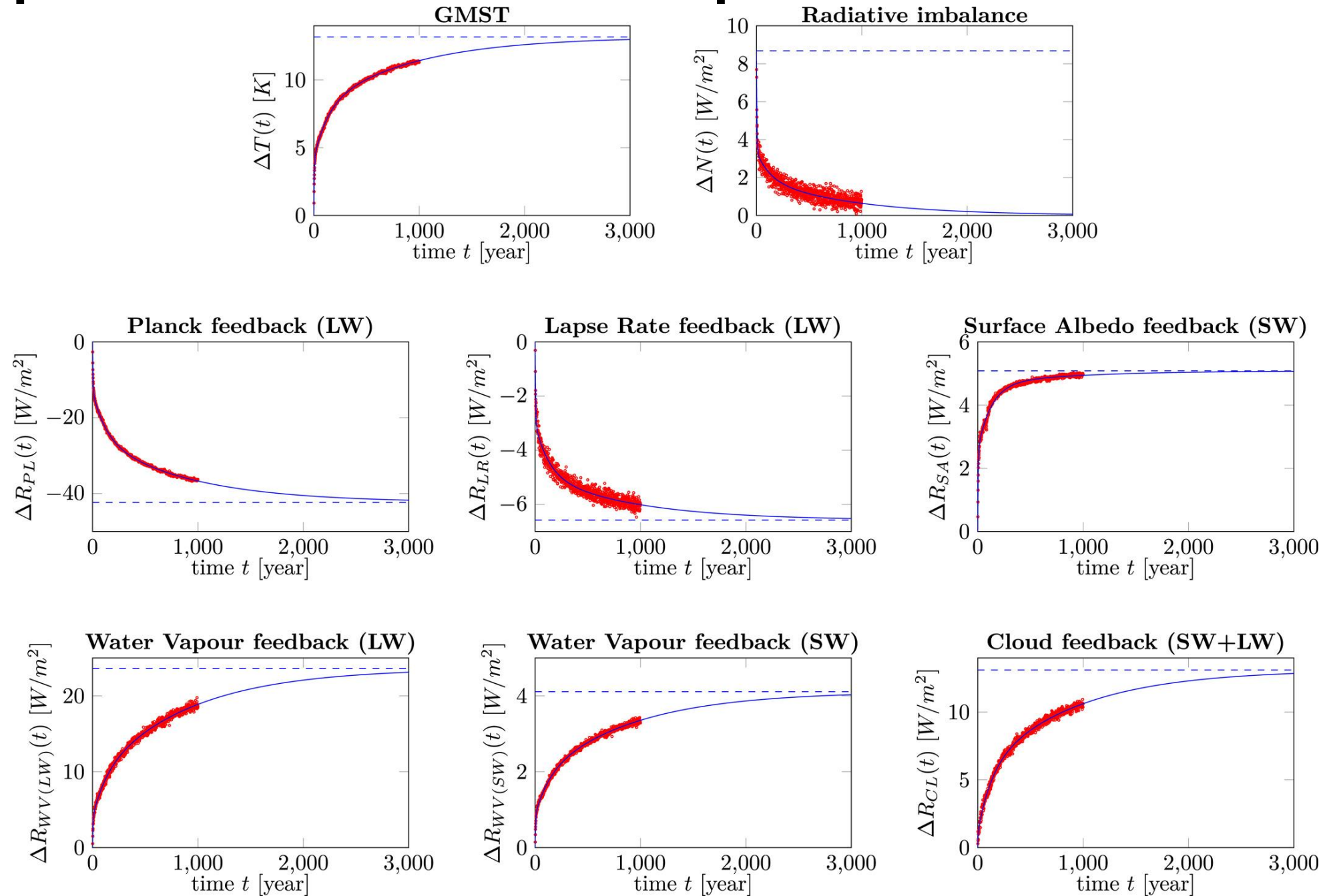
Procedure:

Radiative kernel: CESM-CAM5  
from [Pendergrass et al, 2017]

1. Compute  $\langle \Delta R_j \rangle(t) = \left\langle \frac{\partial \Delta N}{\partial y_j} (\vec{y}_* ; \mu_*) \Delta y_j \right\rangle (t)$
2. Fit  $\langle \Delta R_j \rangle(t) = \sum_{n=1}^M \beta_n^{[R_j]} \mathcal{M}_n^g(t)$  (and similar for  $\Delta T$  and  $N$ )
3. Compute feedback strengths



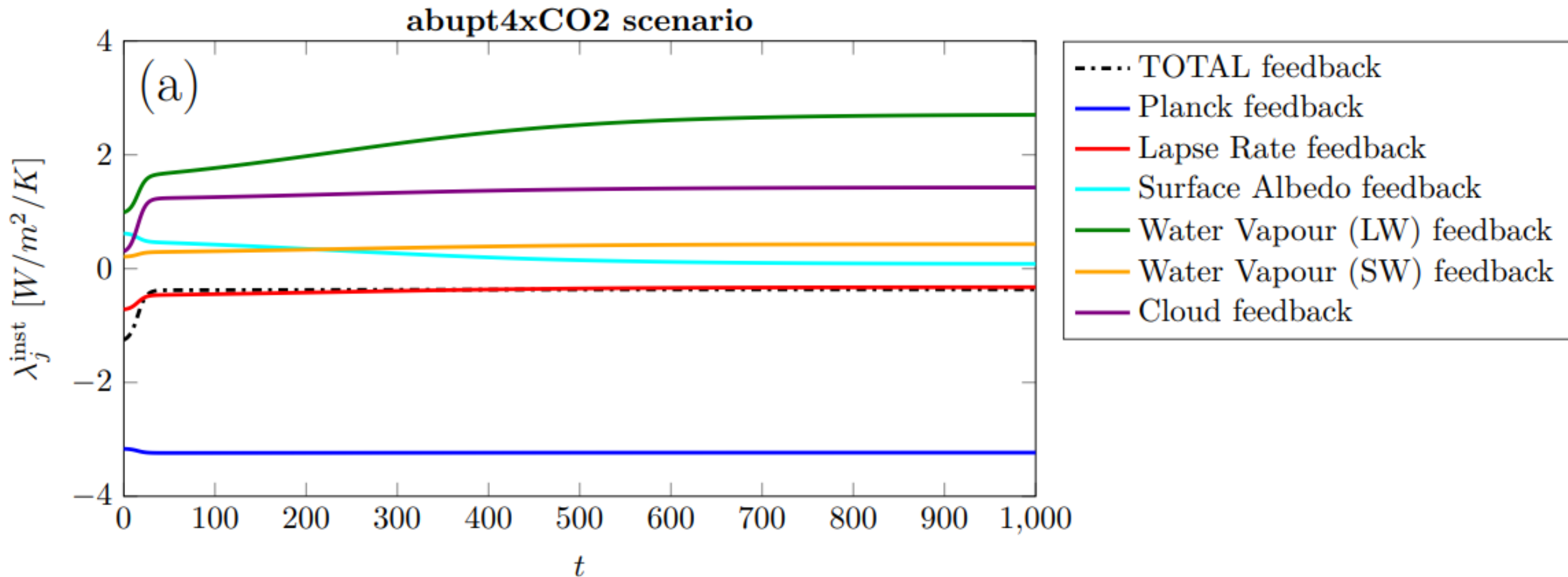
# Application to CESM2's abrupt4xCO2 run in CMIP6 (2)



# Application to CESM2's abrupt4xCO2 run in CMIP6 (3)

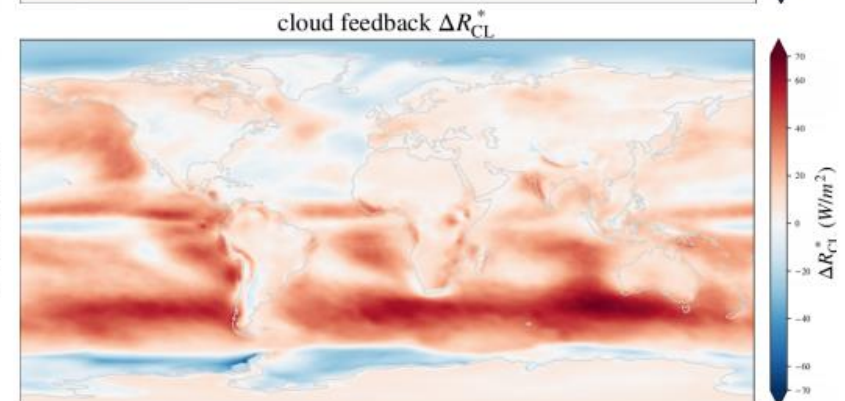
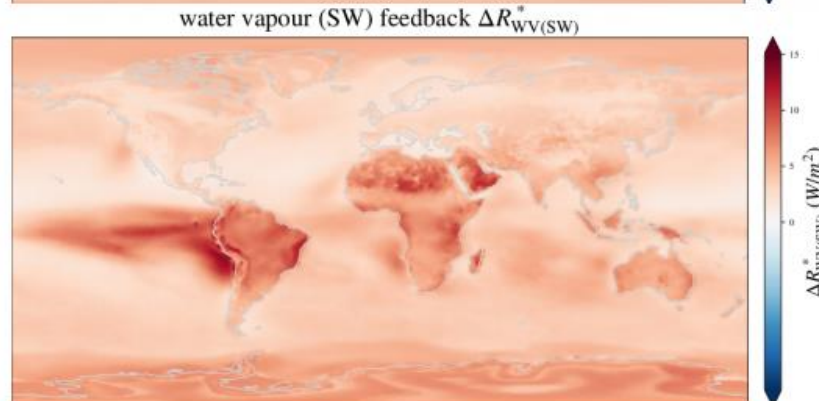
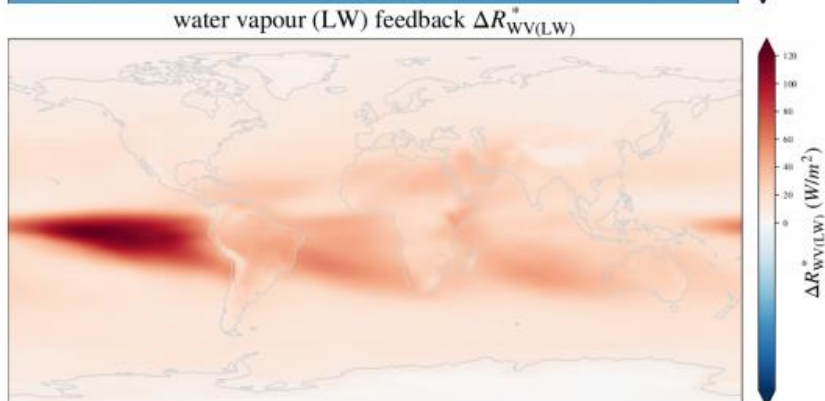
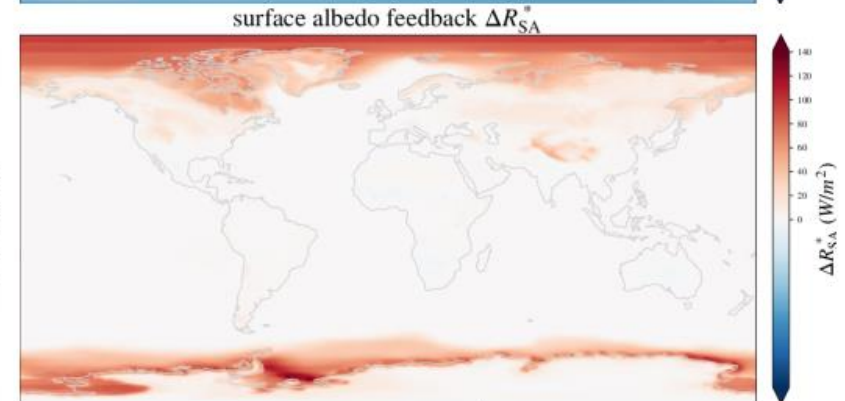
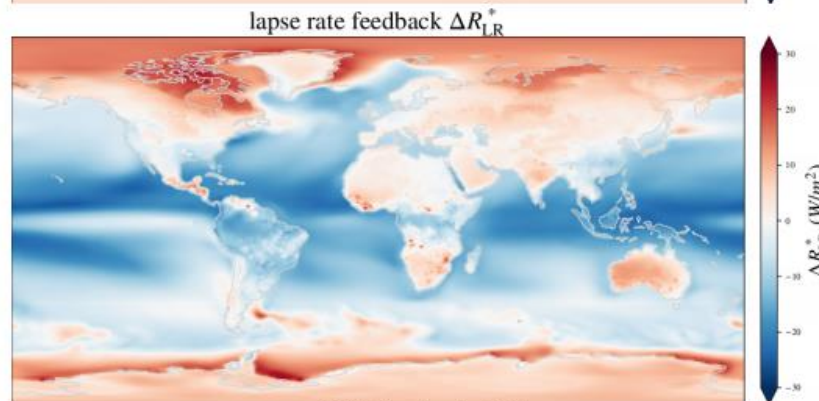
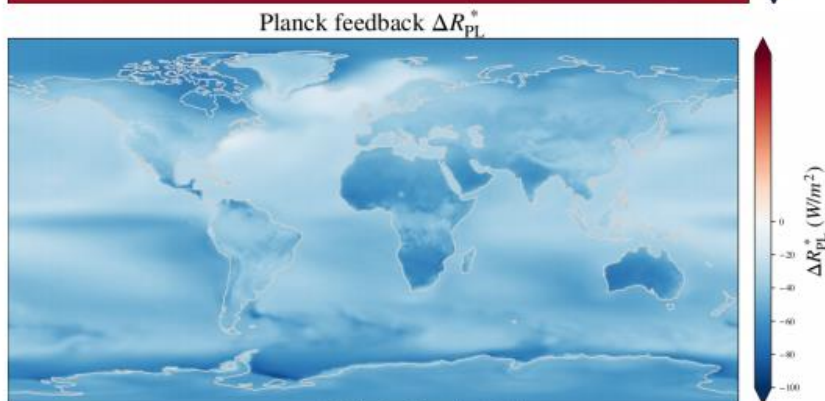
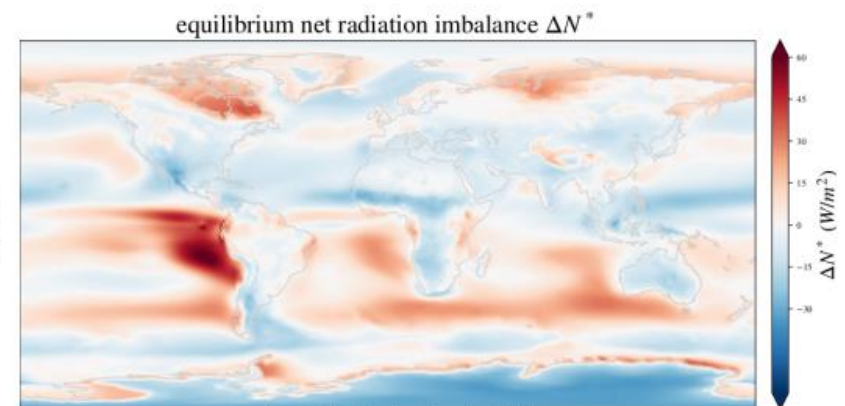
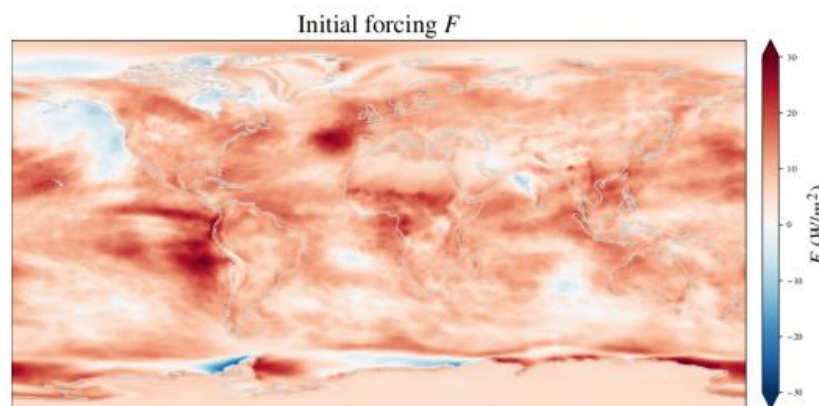
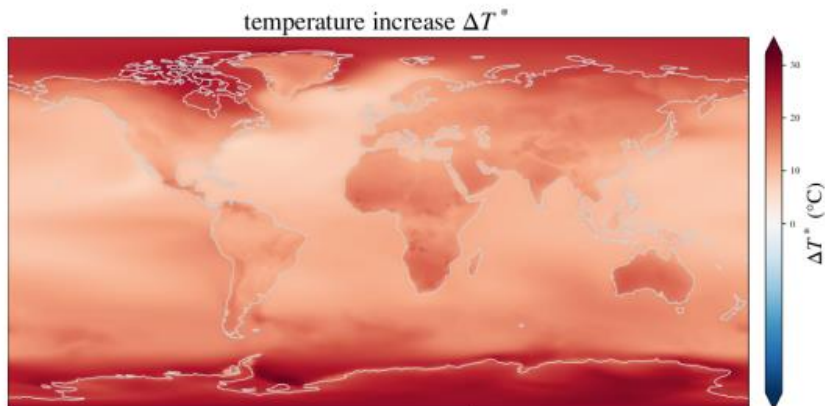
		Mode 1	Mode 2	Mode 3		Equilibrium
$\tau_m$		4.5 ( $\pm$ 0.1)	127 ( $\pm$ 3.8)	889 ( $\pm$ 50)		—
$\lambda_m$		-1.28 ( $\pm$ 0.08)	-0.38 ( $\pm$ 0.03)	-0.37 ( $\pm$ 0.02)		-0.66 ( $\pm$ 0.03)
Planck (LW)		-3.16 ( $\pm$ 0.02)	-3.24 ( $\pm$ 0.02)	-3.23 ( $\pm$ 0.01)		-3.21 ( $\pm$ 0.05)
Lapse Rate (LW)		-0.73 ( $\pm$ 0.03)	-0.50 ( $\pm$ 0.03)	-0.32 ( $\pm$ 0.03)		-0.50 ( $\pm$ 0.01)
Surface Albedo (SW)		+0.62 ( $\pm$ 0.04)	+0.56 ( $\pm$ 0.02)	+0.08 ( $\pm$ 0.10)		+0.39 ( $\pm$ 0.01)
Water Vapour (LW)		+0.97 ( $\pm$ 0.03)	+1.38 ( $\pm$ 0.02)	+2.71 ( $\pm$ 0.01)		+1.79 ( $\pm$ 0.04)
Water Vapour (SW)		+0.21 ( $\pm$ 0.09)	+0.26 ( $\pm$ 0.05)	+0.43 ( $\pm$ 0.02)		+0.31 ( $\pm$ 0.01)
Clouds (SW + LW)		+0.27 ( $\pm$ 0.36)	+1.19 ( $\pm$ 0.02)	+1.43 ( $\pm$ 0.01)		+1.00 ( $\pm$ 0.03)
sum		-1.82 ( $\pm$ 0.37)	-0.36 ( $\pm$ 0.07)	+1.09 ( $\pm$ 0.11)		-0.22 ( $\pm$ 0.08)
residue		+0.54 ( $\pm$ 0.38)	-0.02 ( $\pm$ 0.08)	-1.46 ( $\pm$ 0.11)		-0.43 ( $\pm$ 0.08)

# Application to CESM2's abrupt4xCO2 run in CMIP6 (3)



# Spatial Response – Equilibrium Estimates

$$\Delta R_j(x, t) = \sum_{n=1}^M \beta_n^{[R_j]}(x) \mathcal{M}_n^g(t)$$





# Projections for other forcings

$$\Delta O(t) = \sum_{m=1}^M \beta_m^{[0]} \mathcal{M}_m^g(t)$$



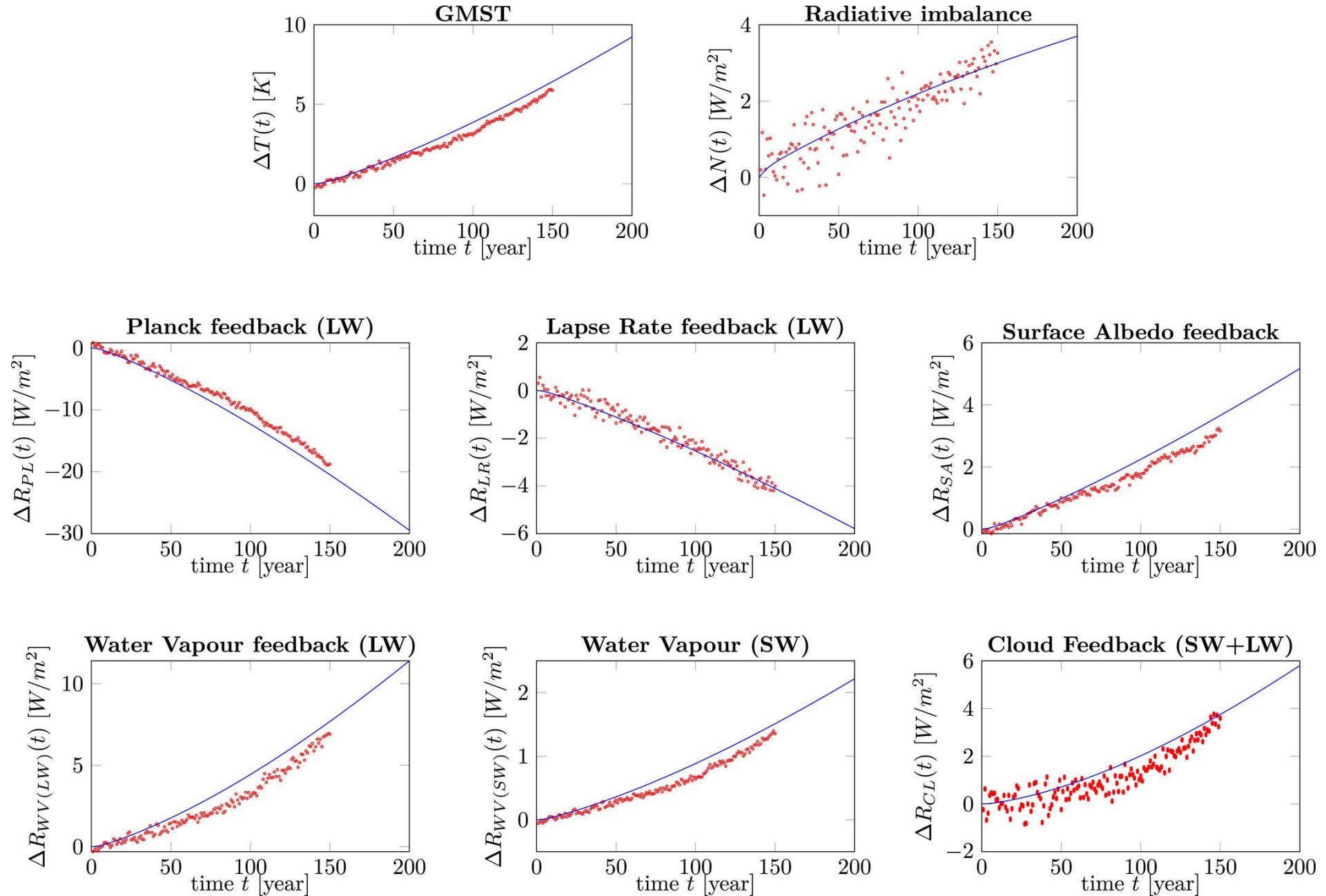
only this gets changed!

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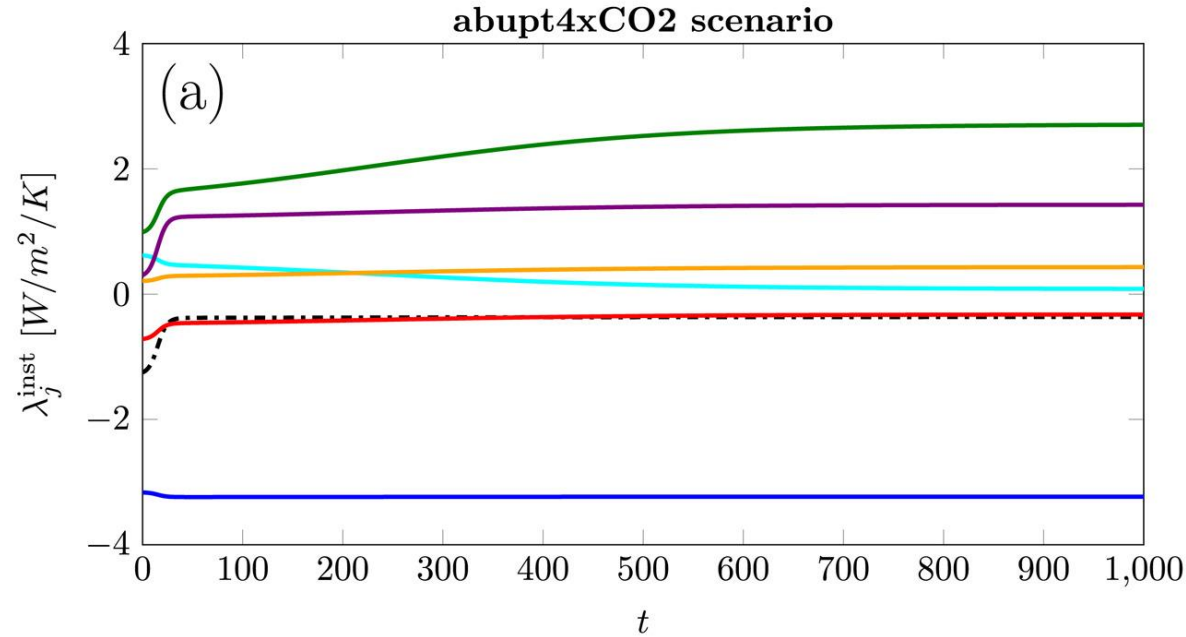
## Linear Response Theory – CAVEATS:

- i. forcings & responses should be ‘small enough’
- ii. should look at ensemble means

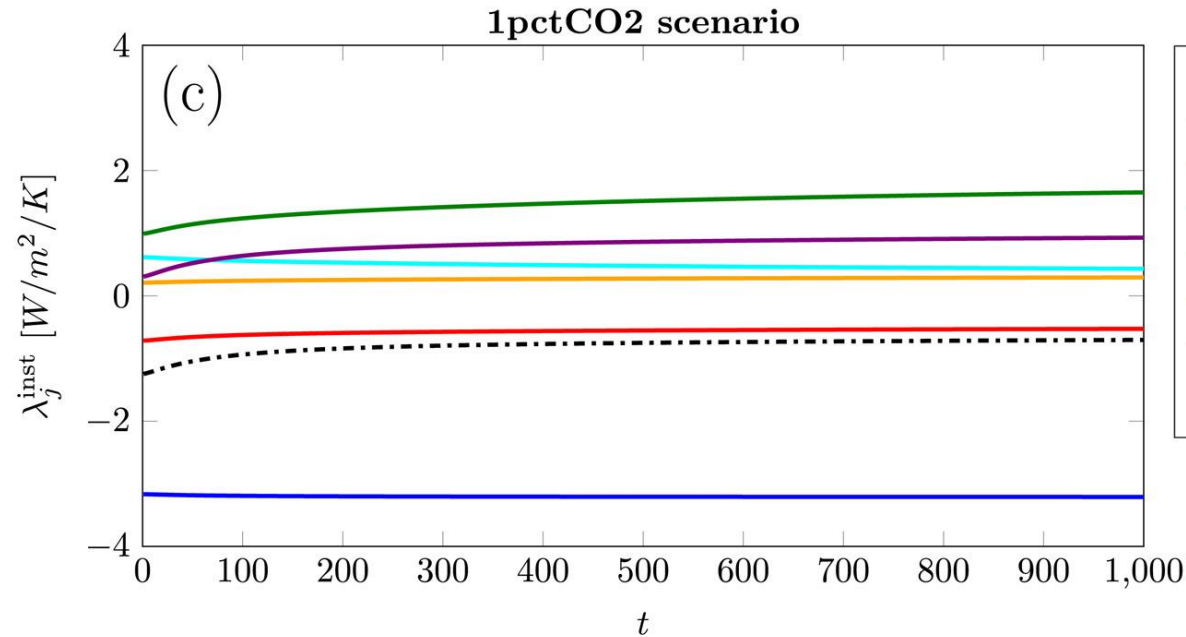
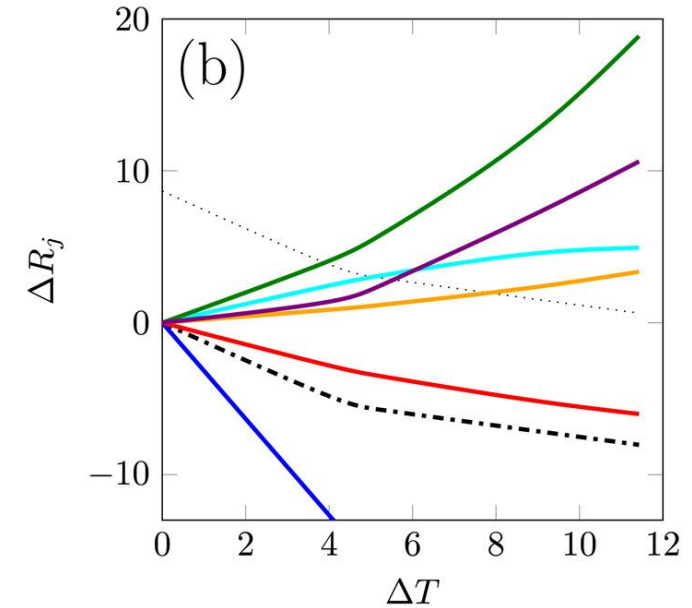
# Projections for CESM2's 1pctCO2 experiment



# Instantaneous feedback strengths for abrupt4xCO2 & 1%CO2



Gregory Plot for abrupt4xCO2 scenario



- TOTAL feedback
- Planck feedback
- Lapse Rate feedback
- Surface Albedo feedback
- Water Vapour (LW) feedback
- Water Vapour (SW) feedback
- Cloud feedback
- ..... TOA imbalance  $\Delta N$

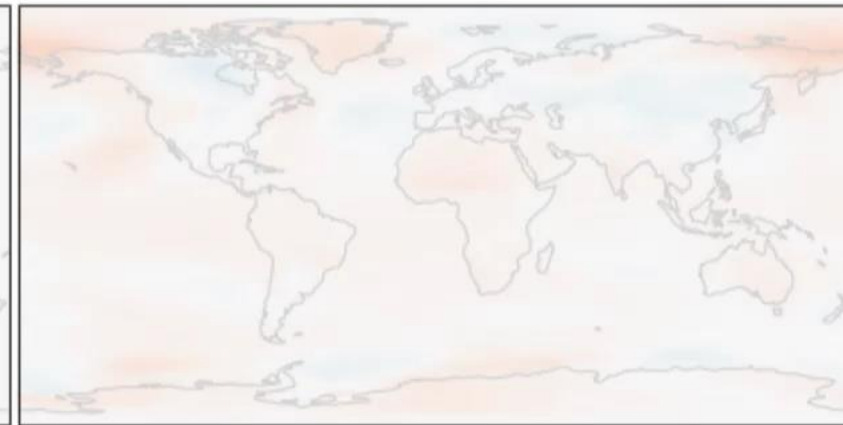
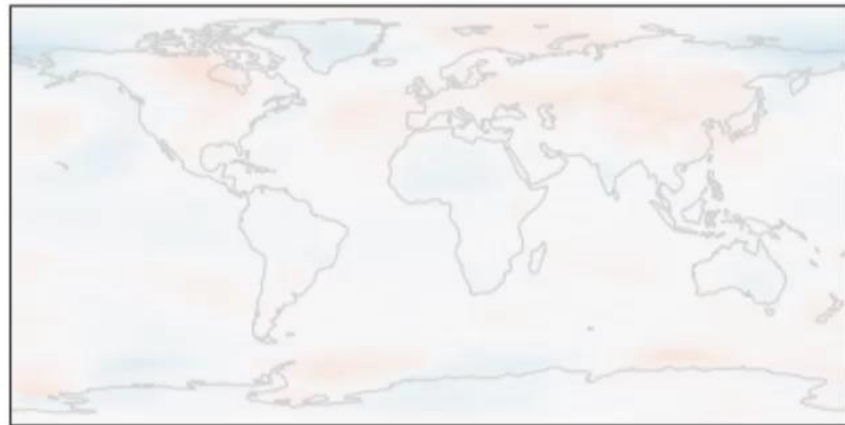
# Spatial projections for 1%CO2 experiment

## TEMPERATURE

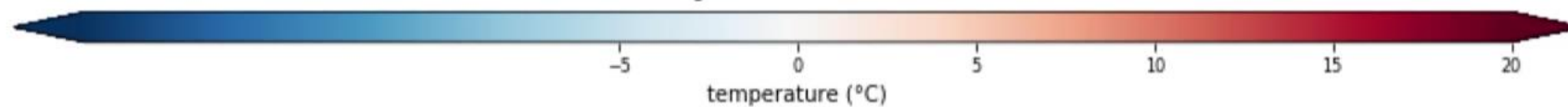
DATA

PROJECTION

ERROR



year = 001



# Spatial projections for 1%CO2 experiment

## SURFACE ALBEDO FEEDBACK CONTRIBUTION

DATA

PROJECTION

ERROR



year = 001



# Spatial projections for 1%CO2 experiment

## WATER VAPOUR (LW) FEEDBACK CONTRIBUTION

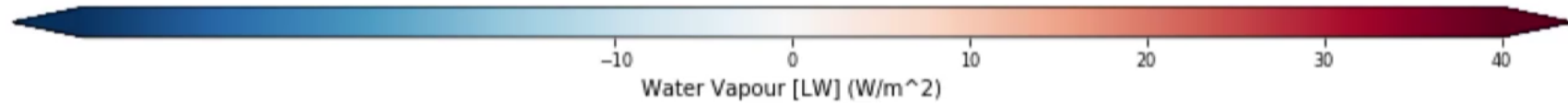
DATA

PROJECTION

ERROR



year = 001



# Projections of Climate Feedbacks

## SUMMARY OF METHOD

Evolution of observable

$$\Delta O(t) = \sum_{m=1}^M \beta_m^{[O]} \mathcal{M}_m^g(t)$$

$$\mathcal{M}_m^g(t) = \int_0^t e^{-s/\tau_m} g(t-s) ds$$

- ☺ Allows dissecting feedback contributions over time and space
  - ★ Feedback strength per mode
  - ★ Feedback missing on long time scale?
- ☺ Projections for other forcings seem possible
  - ★ Tests presented are promising

Paper out in Geophysical Research Letters:

**Projections of the transient state-dependency of climate feedbacks**

Robbin Bastiaansen, Henk A. Dijkstra, Anna S. von der Heydt

