



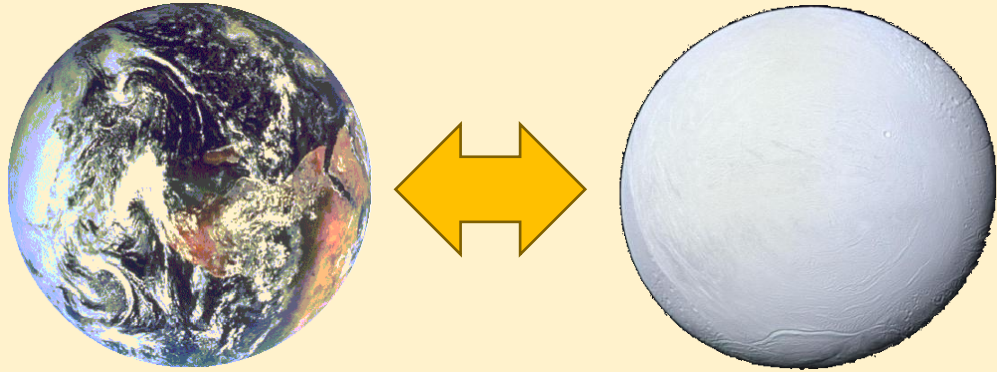
# Fragmented tipping in a spatially heterogeneous world

2022-09-05, NAC 2022

Robbin Bastiaansen (r.bastiaansen@uu.nl)

# Tipping Points

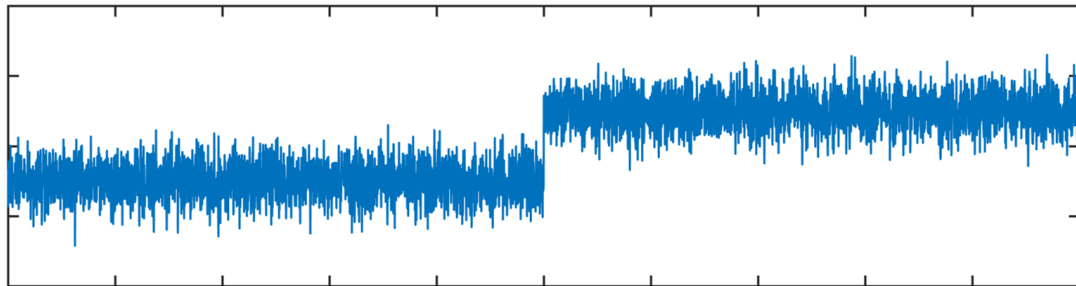
IPCC AR6 (2021) : “a critical threshold beyond which a system reorganizes, often abruptly and/or irreversibly”



Planetary transitions



Ecosystem shifts

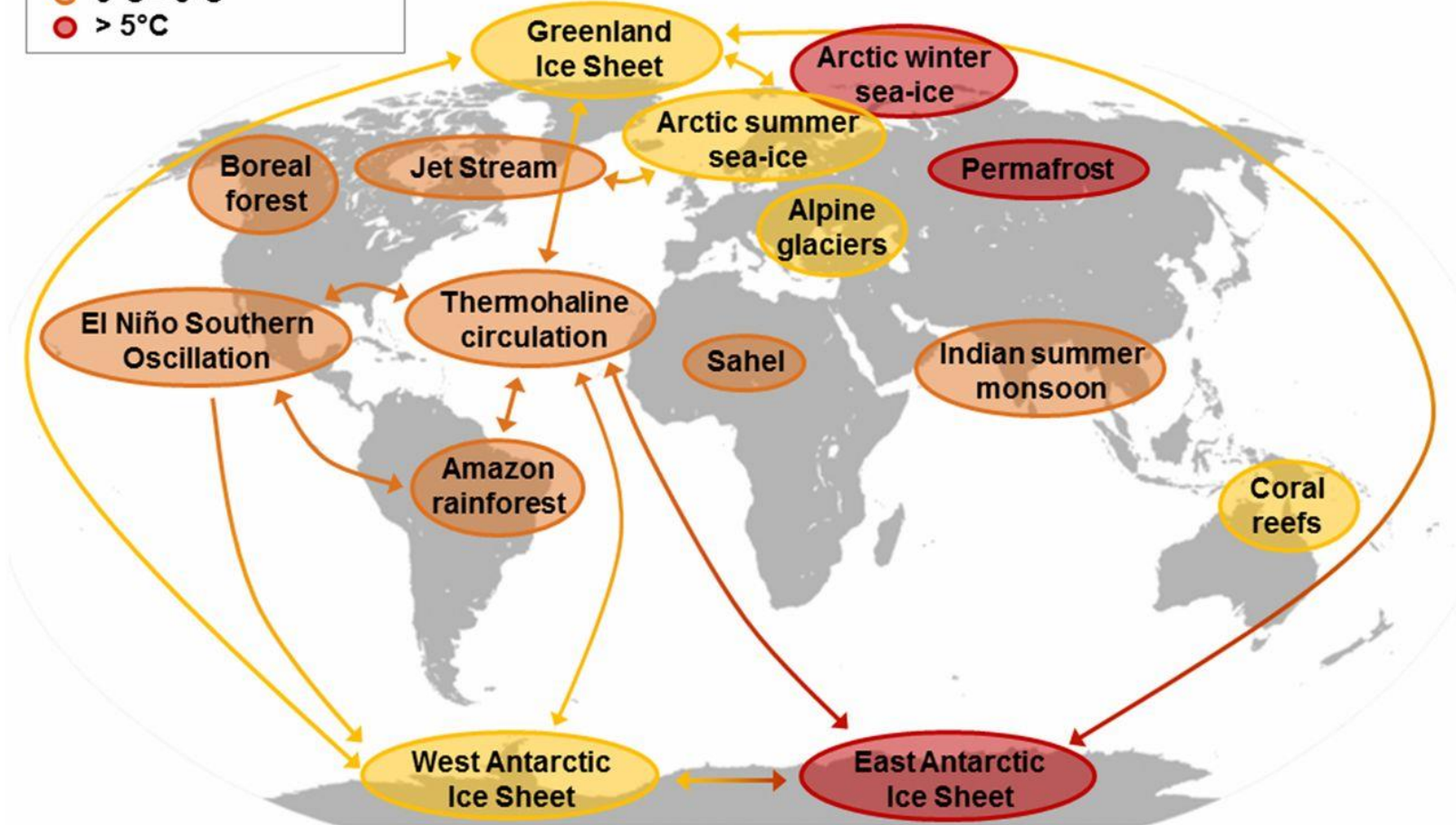


# Tipping Points

IPCC AR6 (2021) : “a critical threshold beyond which a system reorganizes, often abruptly and/or irreversibly”

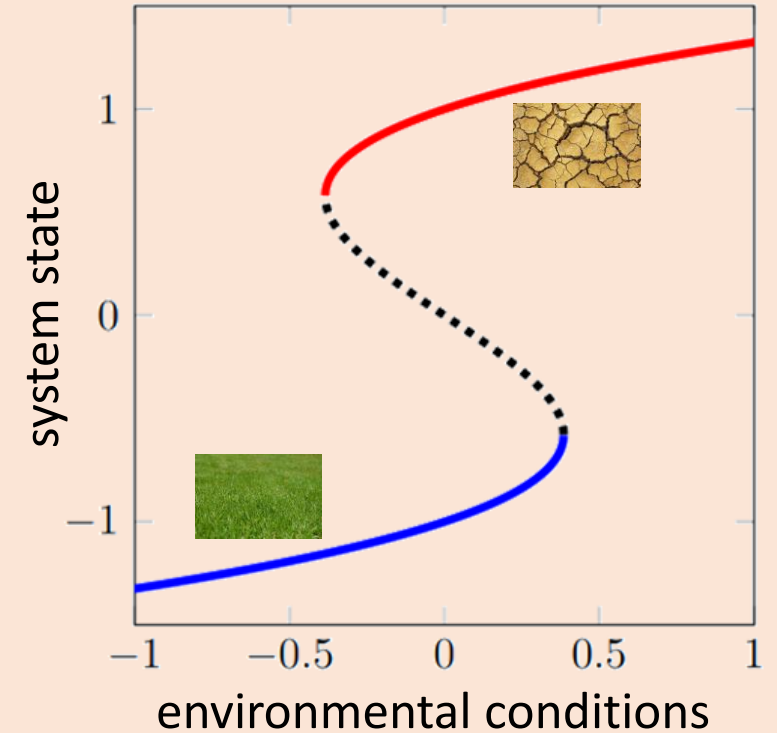
Tipping elements at risk:

- 1°C – 3°C
- 3°C – 5°C
- > 5°C



Tipping points ↔ Bifurcations

$$\frac{dy}{dt} = f(y, \mu)$$





# Reality is not always spatially-uniform!

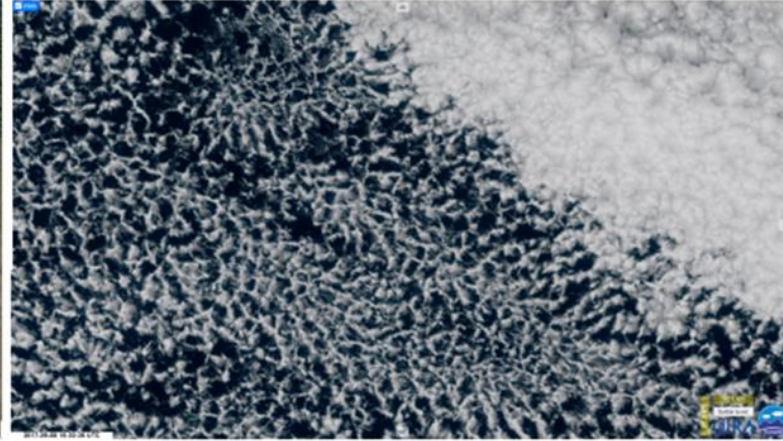
tropical forest  
& savanna  
ecosystems

[Google Earth]



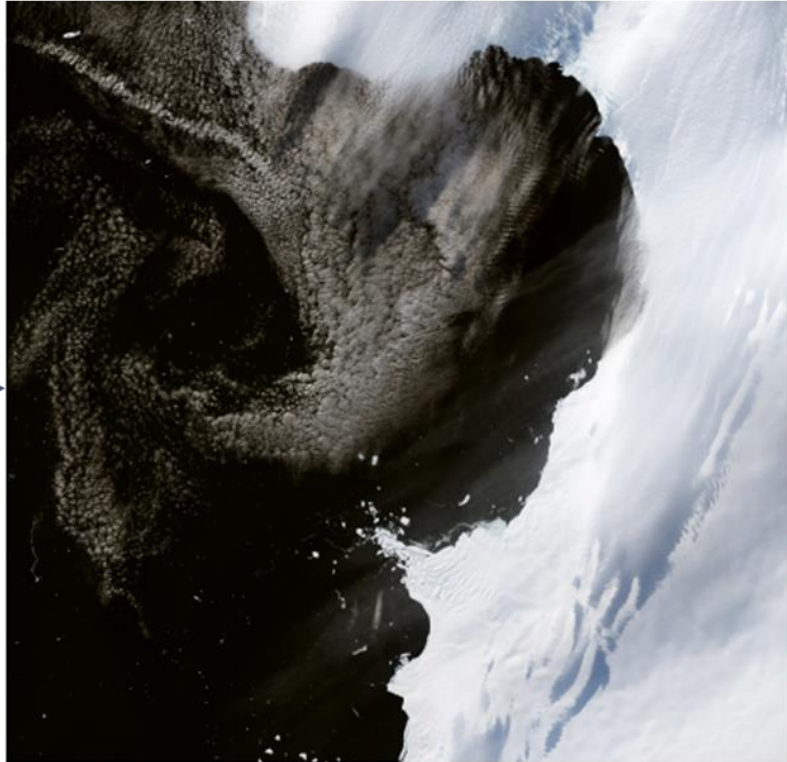
types of  
stratocumulus  
clouds

[RAMMB/CIRA SLIDER]



sea-ice & water  
at Eltanin Bay

[NASA's Earth observatory]



algae bloom  
in Lake St. Clair

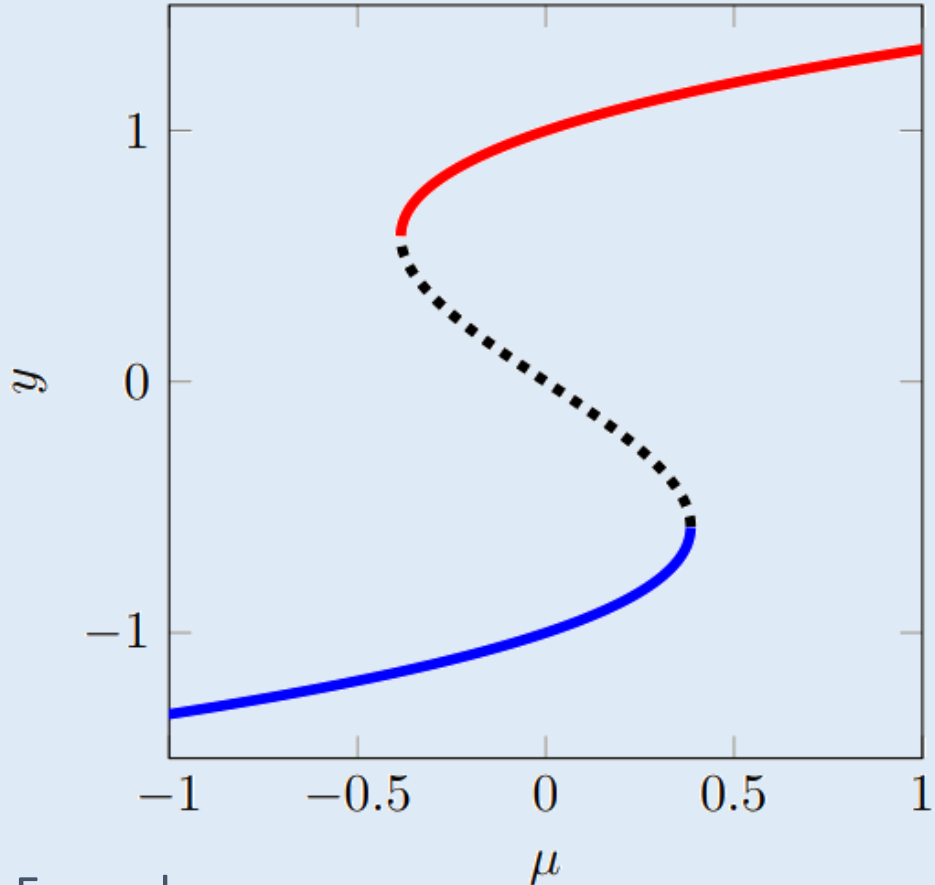
[NASA's Earth observatory]



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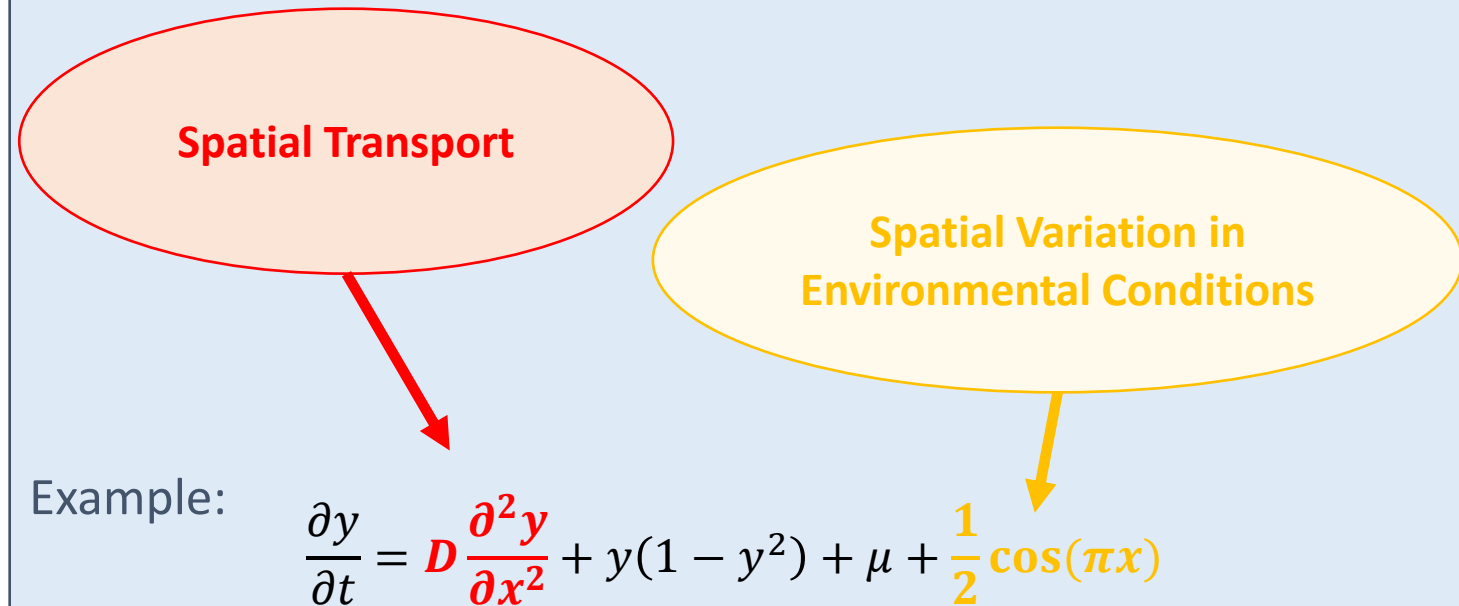
Robbin Bastiaansen (r.bastiaansen@uu.nl), Henk A. Dijkstra and Anna S. von der Heydt

## Classic Tipping



Example:  $\frac{dy}{dt} = y(1 - y^2) + \mu$

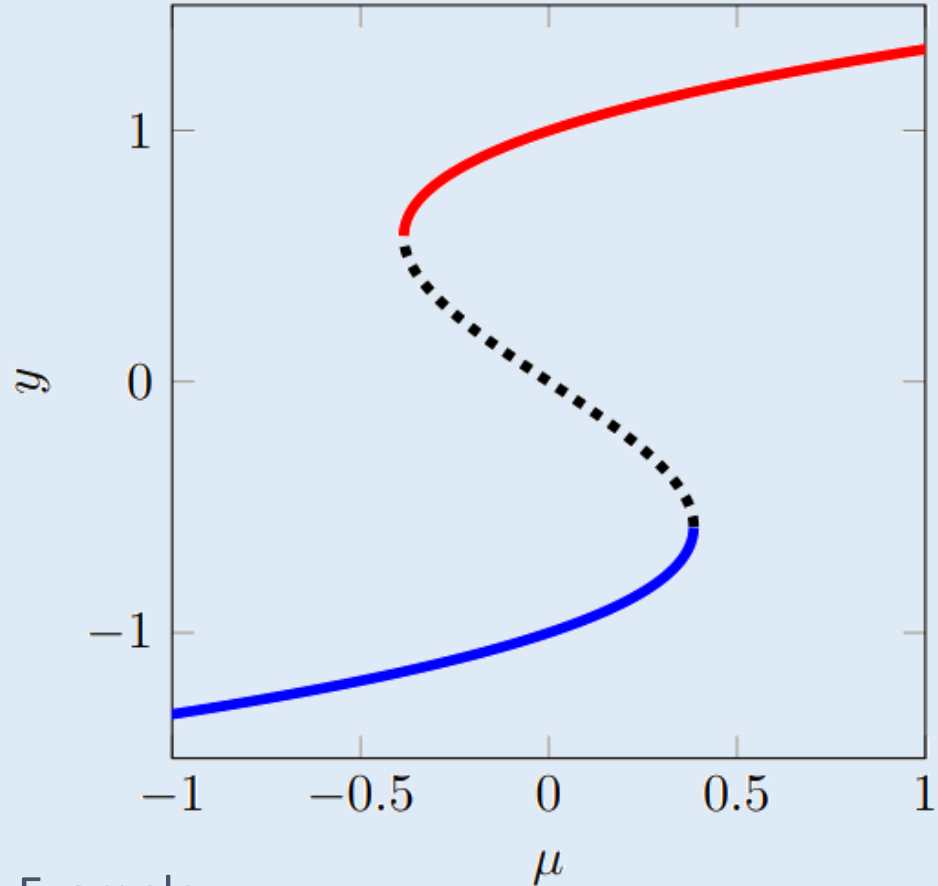
## Tipping in Spatially Heterogeneous Systems



# Fragmented Tipping in a spatially heterogeneous world

Robbin Bastiaansen (r.bastiaansen@uu.nl), Henk A. Dijkstra and Anna S. von der Heydt

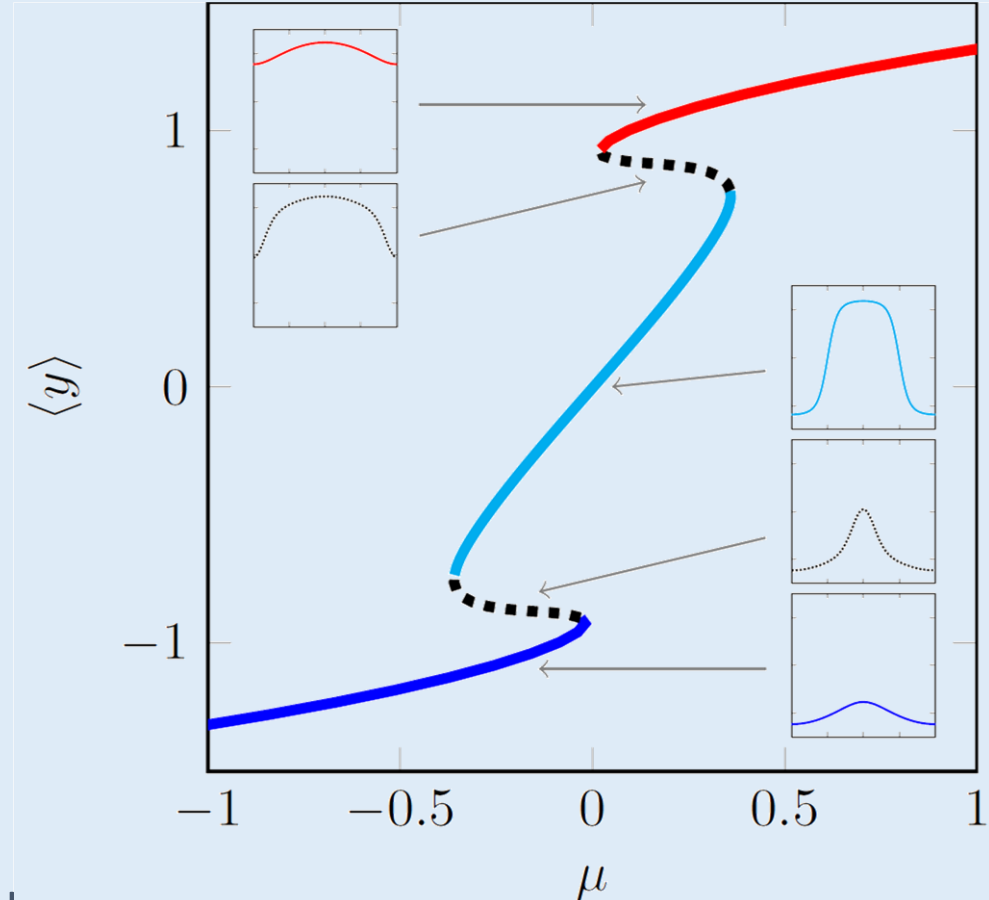
## Classic Tipping



Example:

$$\frac{dy}{dt} = y(1 - y^2) + \mu$$

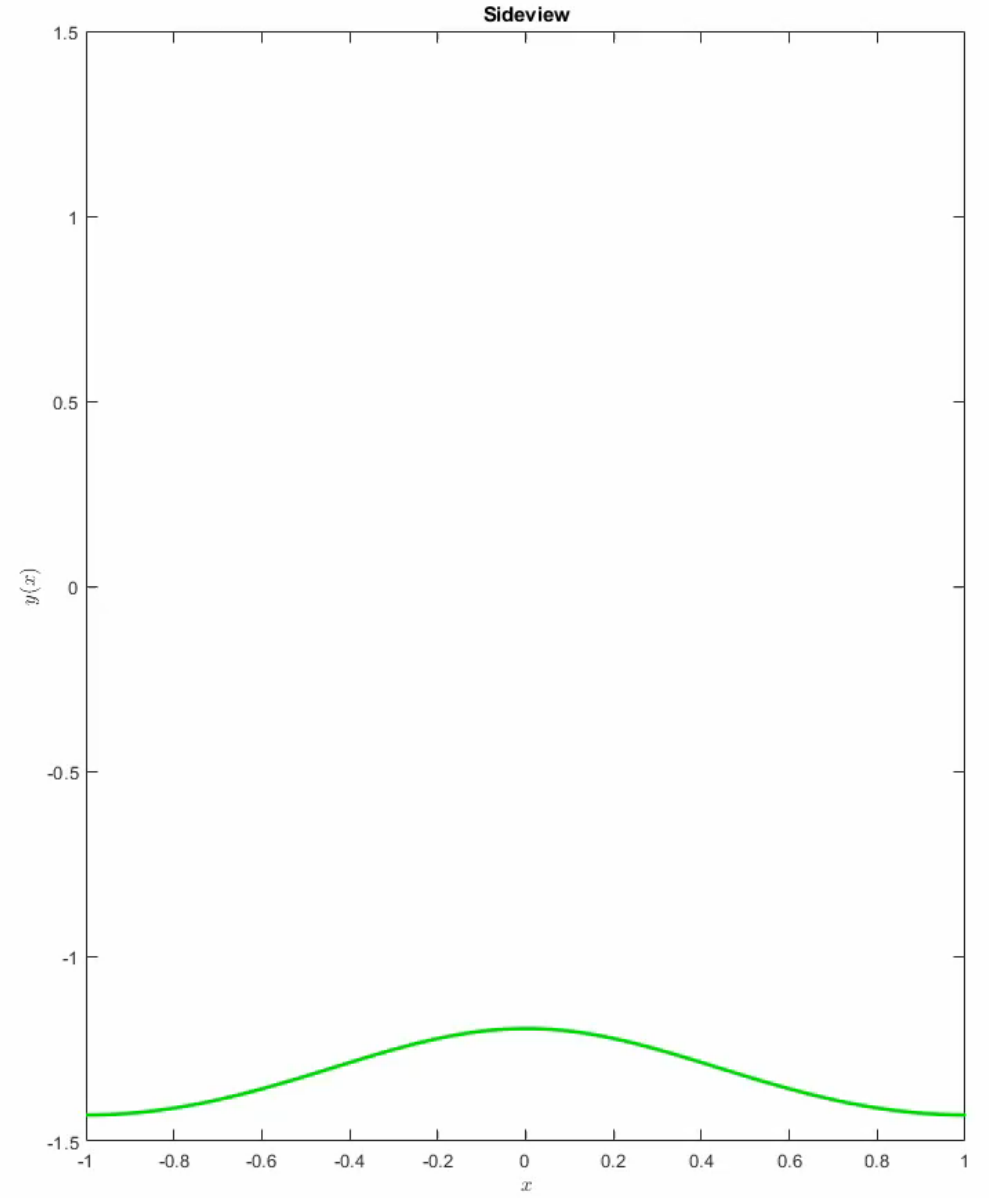
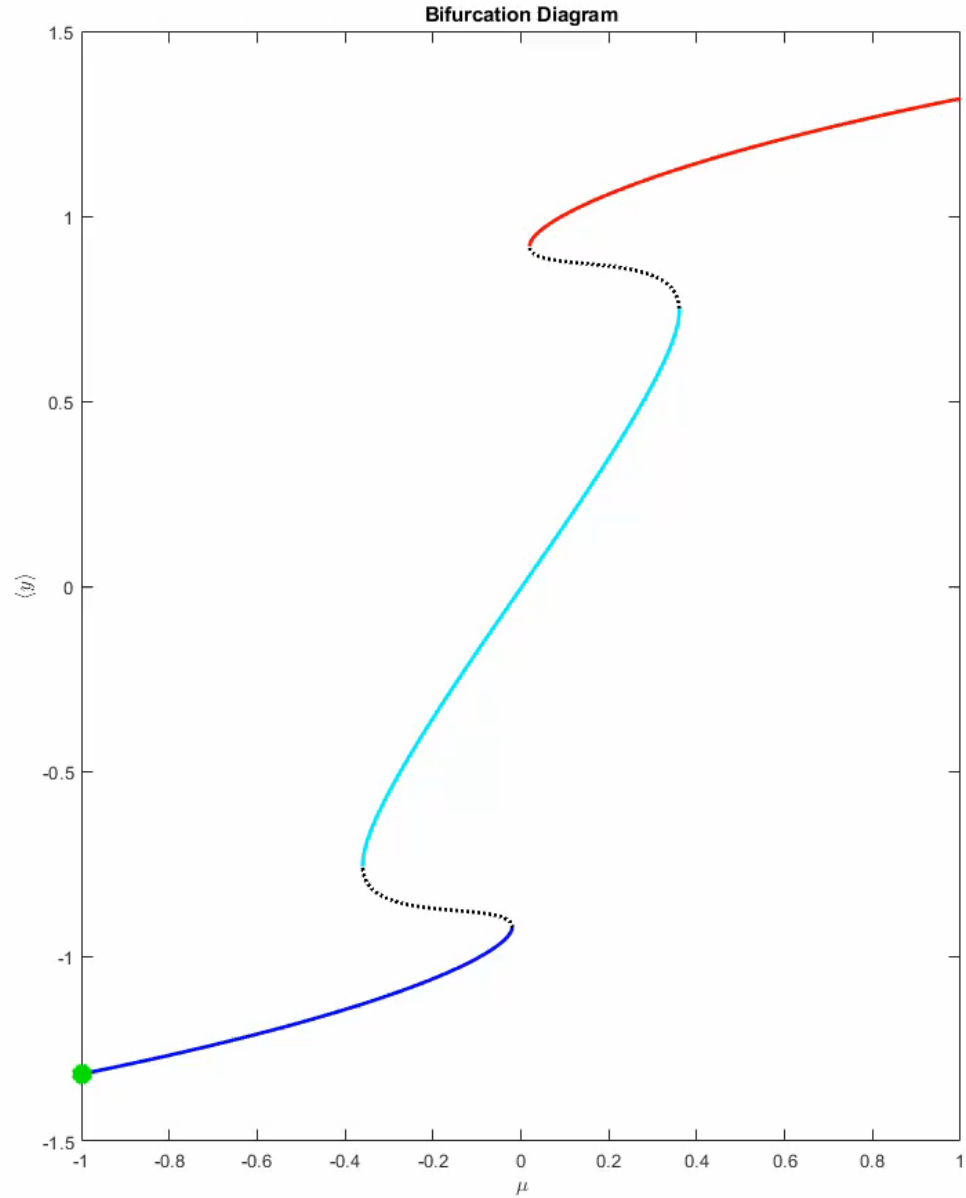
## Tipping in Spatially Heterogeneous Systems



Example:

$$\frac{\partial y}{\partial t} = D \frac{\partial^2 y}{\partial x^2} + y(1 - y^2) + \mu + \frac{1}{2} \cos(\pi x)$$

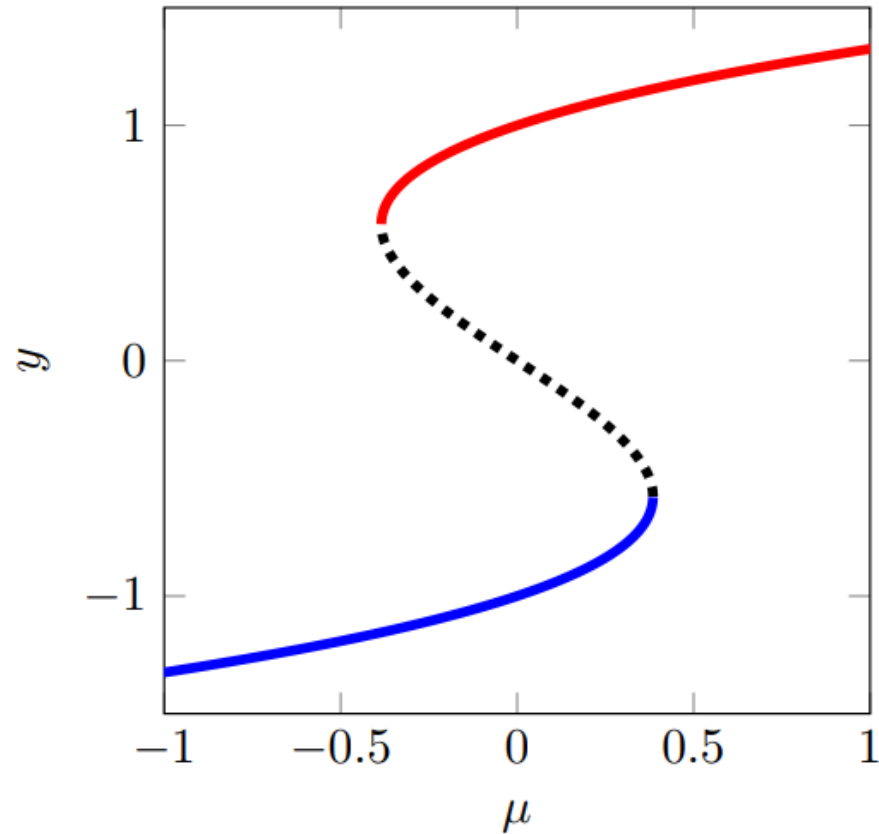
# Fragmented Tipping





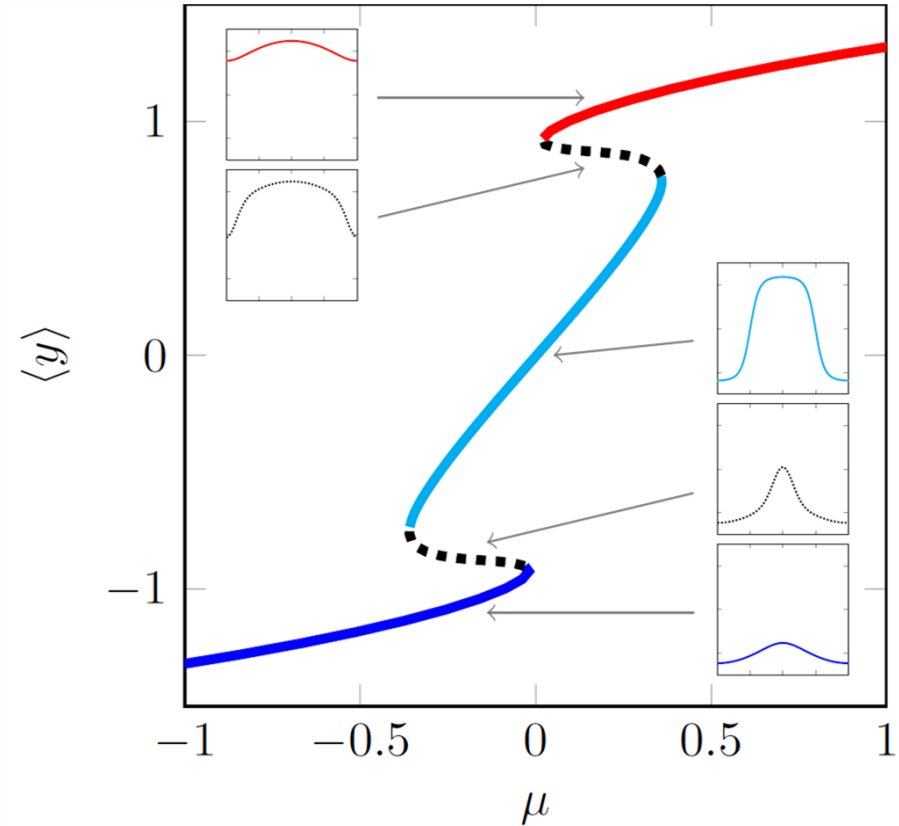
# Fragmented Tipping

Classic picture



Tipping leads to full reorganisation

New picture



Fragmented tipping possible:  
Only part of the domain reorganises

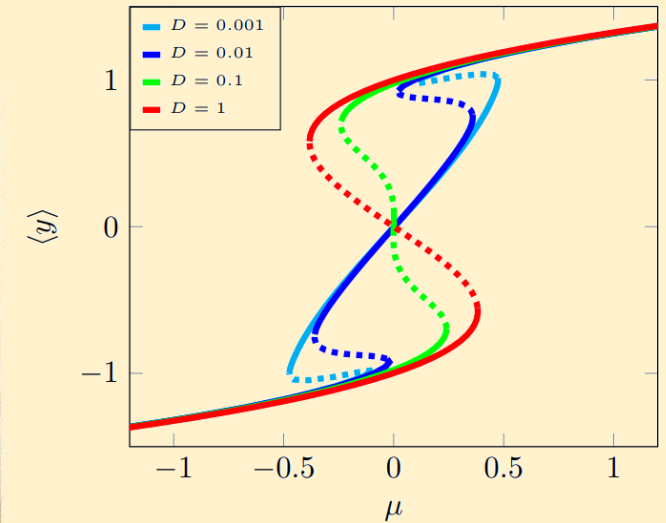
# Do systems always behave like this? (a.k.a. the small print)

No.

Well-mixed systems



Spatially confined systems

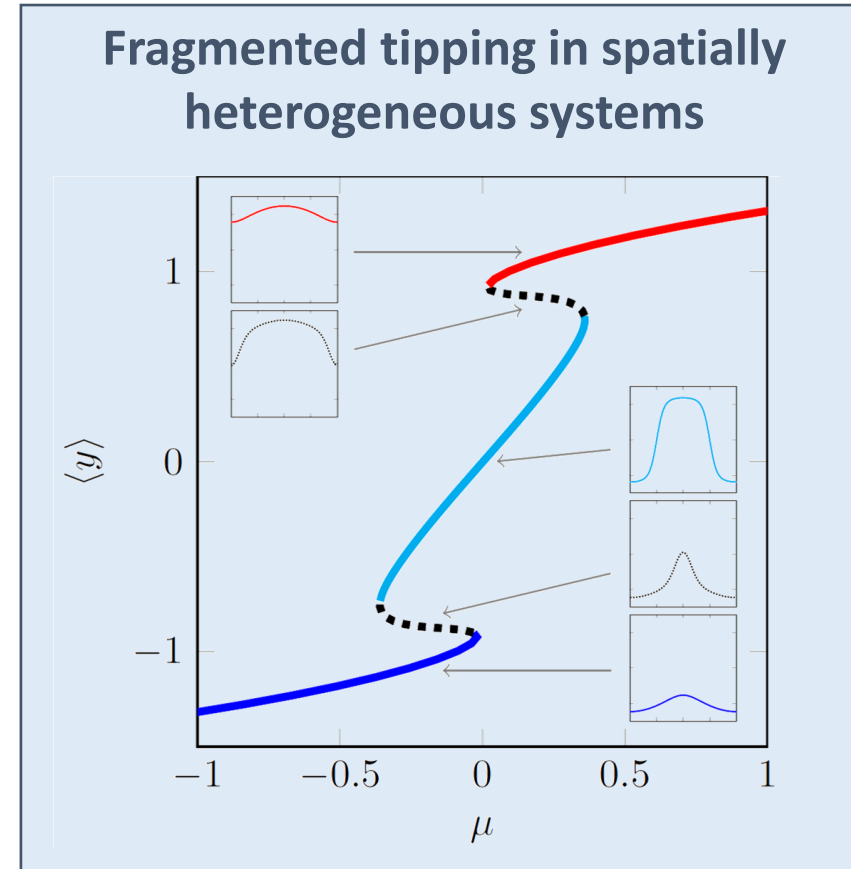
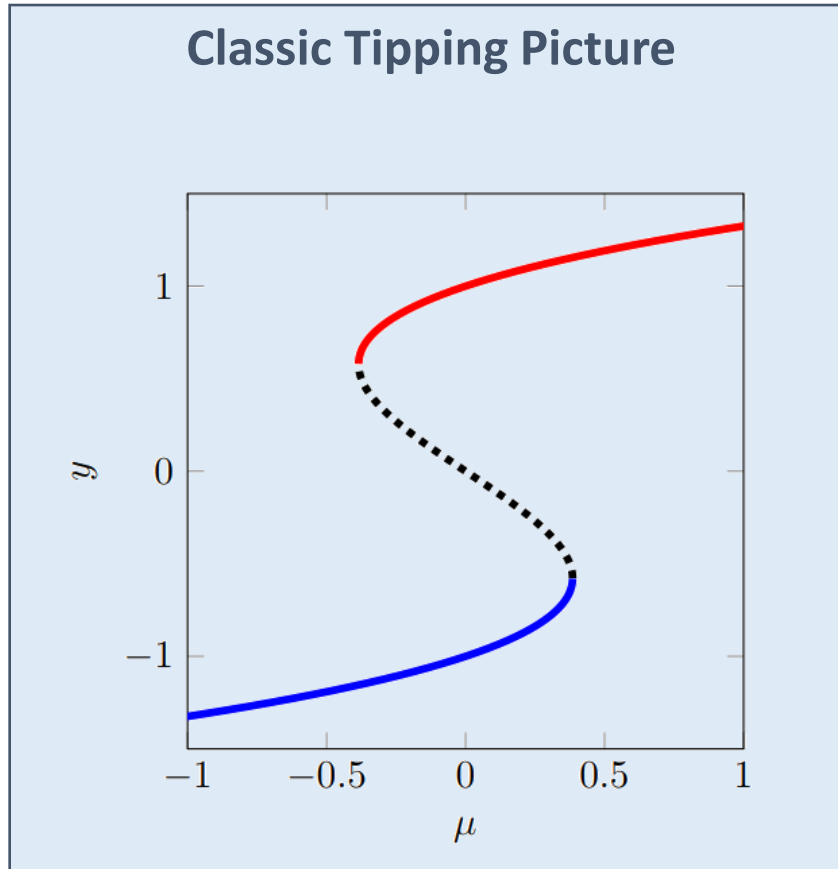


→ Such systems (again) just have one global tipping point ←

But even in other systems terms & conditions apply:  
System-specific knowledge is required!

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Bastiaansen, R., Dijkstra, H. A., & von der Heydt, A. S. (2022).  
 Fragmented tipping in a spatially heterogeneous  
 world. *Environmental Research Letters*, 17, 045006



